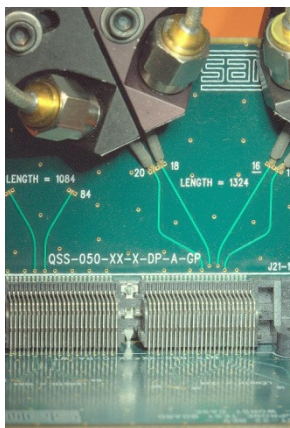
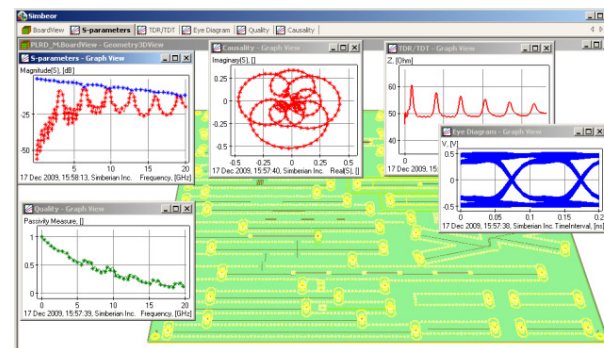


# Quality of High Frequency Measurements: Practical Examples, Theoretical Foundations, and Successful Techniques that Work Past the 40GHz Realm

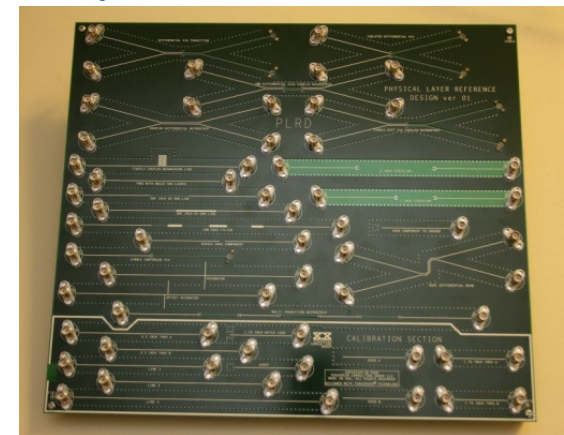
*Samtec-Simberian-Teraspeed  
Tutorial for DesignCon2010  
Tom Dagostino, Teraspeed Consulting Group  
Yuriy Shlepnev, Simberian Inc.*



2/8/2010



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# What we show

- ❑ Even well calibrated VNA measurements have significant quality issues
  - Passivity and reciprocity violations
  - Causality problems due to noise and glitches or anomalies due to multi-line calibration (TRL)
- ❑ Building Rational Compact Models (RCM) resolves the key quality issues
  - Passivity/causality improvements
  - Good correspondence in frequency and in time domains

$$S_{i,j}(\omega) = \left[ d_{ij} + \sum_{n=1}^{N_{ij}} \left( \frac{r_{ij,n}}{i\omega - p_{ij,n}} + \frac{r_{ij,n}^*}{i\omega - p_{ij,n}^*} \right) \right] \cdot e^{-i\omega T_{ij}}$$

## If you happen to...

---

- ❑ Build interconnect models for internal use
- ❑ Send interconnect models to customers developing consumer products
- ❑ Confirm models with measurements or electromagnetic analysis
- ❑ Use models for compliance level testing
- ❑ ...

You need to have ...

# Pristine S-parameters

- Reciprocal (no non-linear or anisotropic materials)

$$S_{i,j} = S_{j,i} \text{ or } S = S^t$$

- Passive (interconnects do not generate energy)

$$P_{in} = \bar{a}^* \cdot [U - S^* S] \cdot \bar{a} \geq 0 \quad \Rightarrow \quad \text{eigenvals}[S^* \cdot S] \leq 1$$

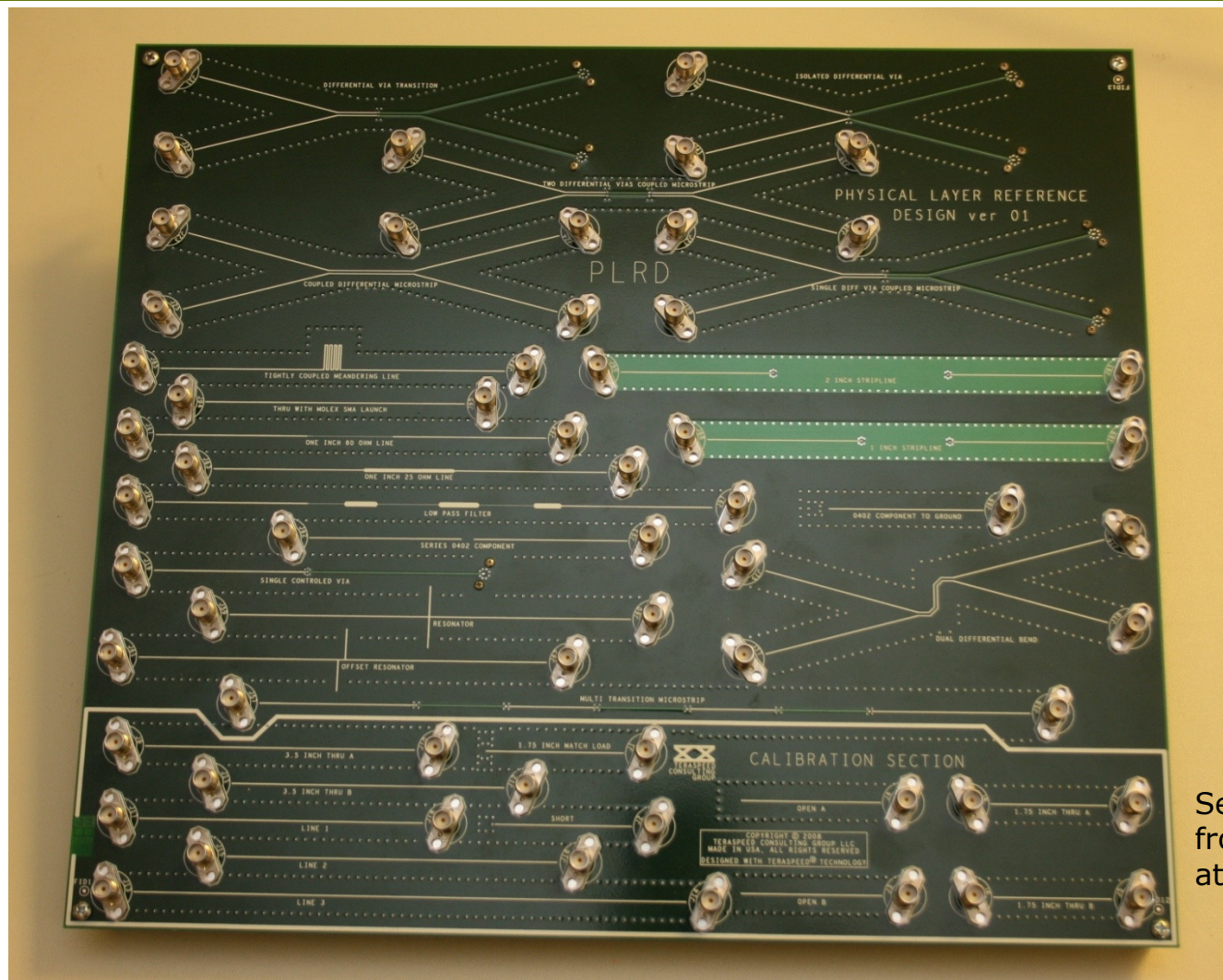
- Causal – no response before the excitation or

$$S_{i,j}(t) = 0, \quad t < T_{ij}$$

- Otherwise your simulation is not reliable and may be even not possible due to stability issues



# Getting Started: PLRD-1 calibration and benchmarking board from Teraspeed Consulting Group



See details in our papers from DesignCon2009 and at DesignCon2010

# We noticed some **BAD** problems with even good data!

## Report for SOLT calibrated measurements

Project1.SOLT_1_INCH_STRIPLINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.61%; SymmetryQM=69.96%; CausalityQM=31.3%
Project1.SOLT_2_INCH_STRIPLINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.85%; SymmetryQM=72.11%; CausalityQM=41.2%
Project1.SOLT_COUPLED_DIFFERENTIAL_MICROSTRIP_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9967%; ReciprocityQM=99.35%; SymmetryQM=73.76%; CausalityQM=6.9%
Project1.SOLT_DIFFERENTIAL_VIA_TRANSITION_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9969%; ReciprocityQM=99.35%; SymmetryQM=67.64%; CausalityQM=11.1%
Project1.SOLT_DUAL_DIFFERENTIAL_BEND_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9966%; ReciprocityQM=99.35%; SymmetryQM=75.68%; CausalityQM=4.4%
Project1.SOLT_ISOLATED_DIFFERENTIAL_VIA_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9962%; ReciprocityQM=99.34%; SymmetryQM=45.31%; CausalityQM=7.4%
Project1.SOLT_LOW_PASS_FILTER_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=99.32%; CausalityQM=82.1%
Project1.SOLT_MULTI_TRANSITION_MICROSTRIP_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=99.24%; SymmetryQM=70.57%; CausalityQM=62.8%
Project1.SOLT_OFFSET_RESONATOR_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.86%; SymmetryQM=39.01%; CausalityQM=80.5%
Project1.SOLT_RESONATOR_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.91%; SymmetryQM=31.21%; CausalityQM=75.8%
Project1.SOLT_ONE_INCH_25_OHM_LINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.5%; SymmetryQM=57.84%; CausalityQM=54.5%
Project1.SOLT_ONE_INCH_80_OHM_LINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.52%; SymmetryQM=69.36%; CausalityQM=40.7%
Project1.SOLT_SINGLE_CONTROLLED_VIA_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.38%; SymmetryQM=72.05%; CausalityQM=9.5%
Project1.SOLT_SINGLE_DIFF_VIA_COUPLED_MICROSTRIP_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9967%; ReciprocityQM=99.33%; SymmetryQM=66.84%; CausalityQM=13.1%
Project1.SOLT_THRU_WITH_MOLOEX_LAUNCH_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.16%; SymmetryQM=80.57%; CausalityQM=26.5%
Project1.SOLT_TIGHTLY_COUPLED_MEANDERING_LINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=99.09%; SymmetryQM=53.75%; CausalityQM=64.2%
Project1.SOLT_TWO_DIFFERENTIAL_VIAS_COUPLED_MICROSTRIP_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9971%; ReciprocityQM=99.4%; SymmetryQM=65.49%; CausalityQM=29.3%

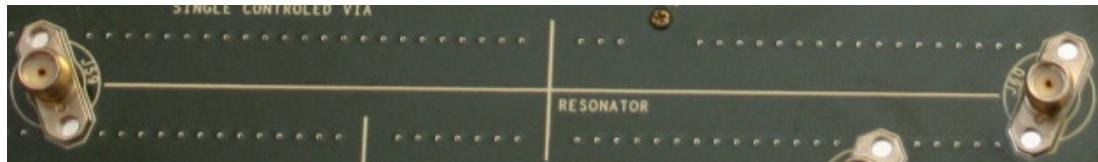
Fixable low causality measure due to noise in small reflection coefficients

Passivity and Reciprocity are OK  
Non-symmetry is due to non-symmetry of the physical structures



# S-parameters for a high-reflection structure: Resonator, SOLT calibration (crash test)

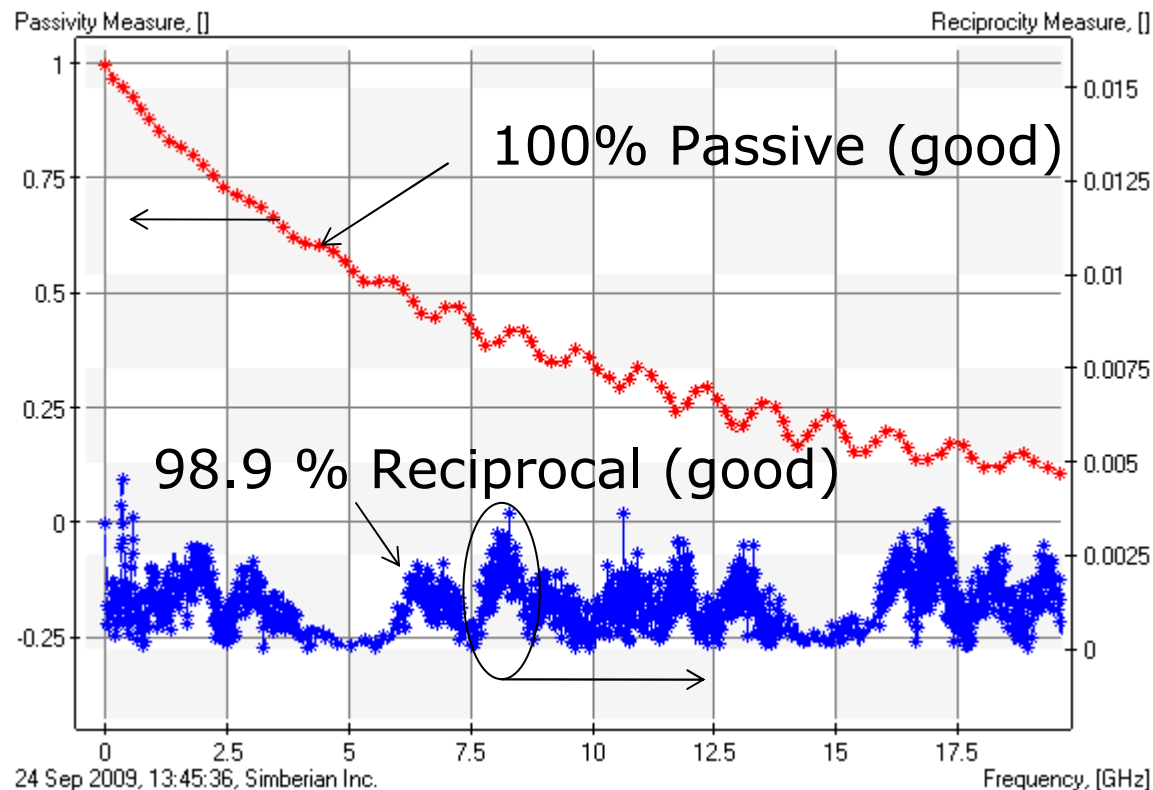
Port 1



Port 2

Project1.SOLT\_RESONATOR\_s2p.Simulation1

MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.91%; SymmetryQM=31.21%; CausalityQM=75.8%



Causality is also OK

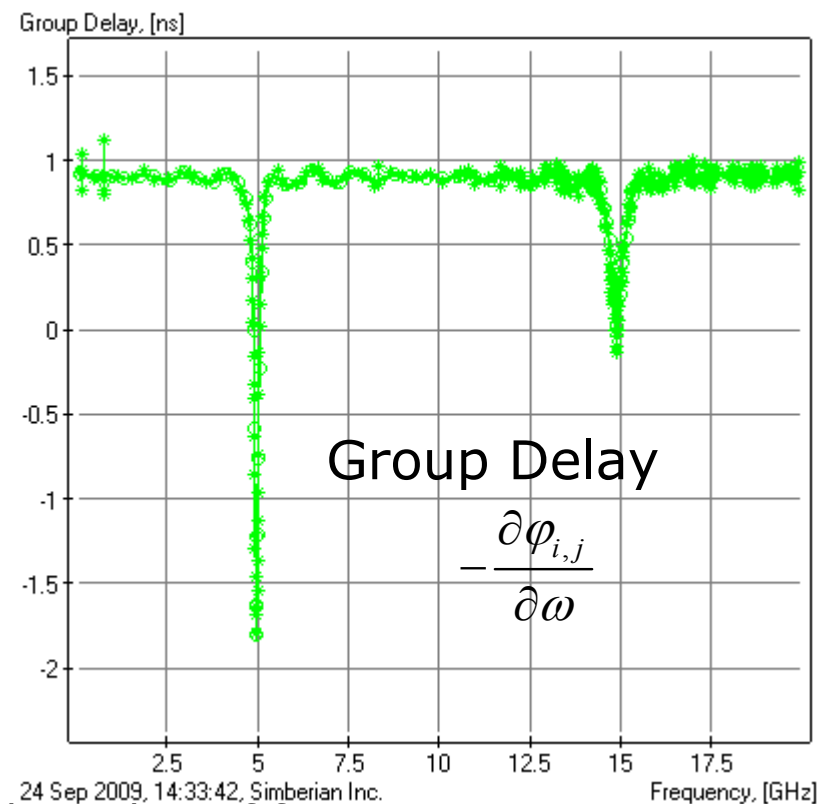
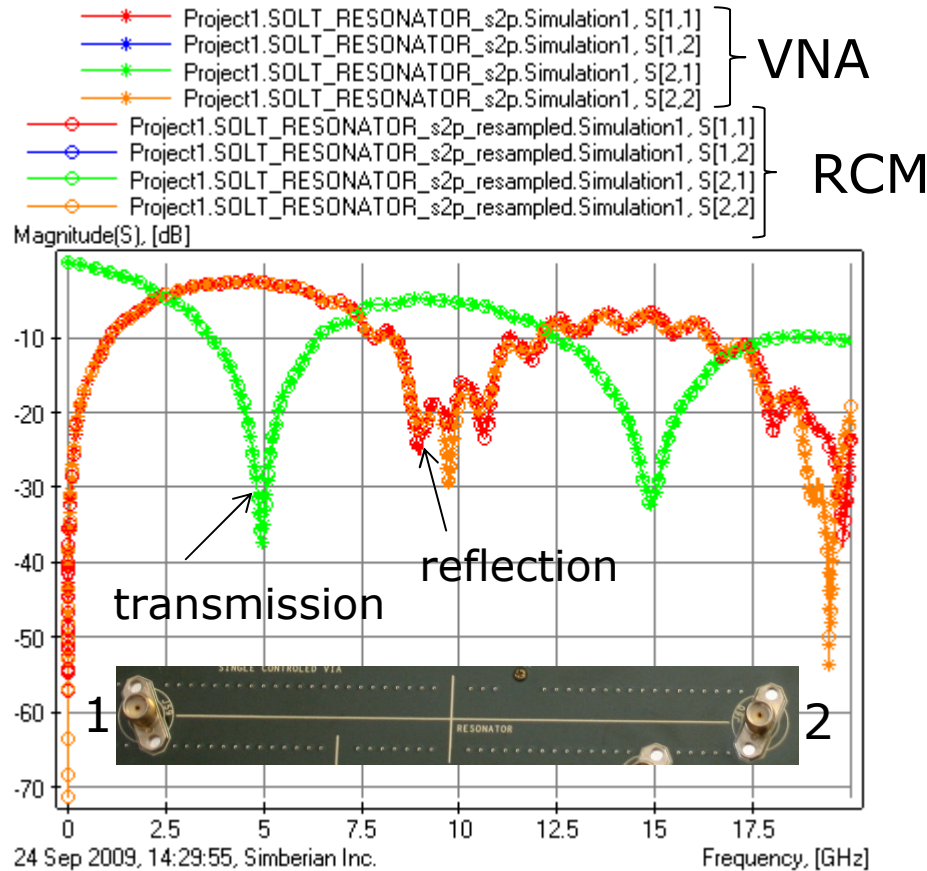
Practically nothing to improve, but what about extrapolation and consistent time-domain analysis

# Resonator (SOLT): RCM for S-parameters

$$S_{i,j} = |S_{i,j}| \cdot \exp(i\varphi_{i,j})$$

RCM model RMS Error is 0.003 (very good)

Passive from DC to infinity, causal and reciprocal

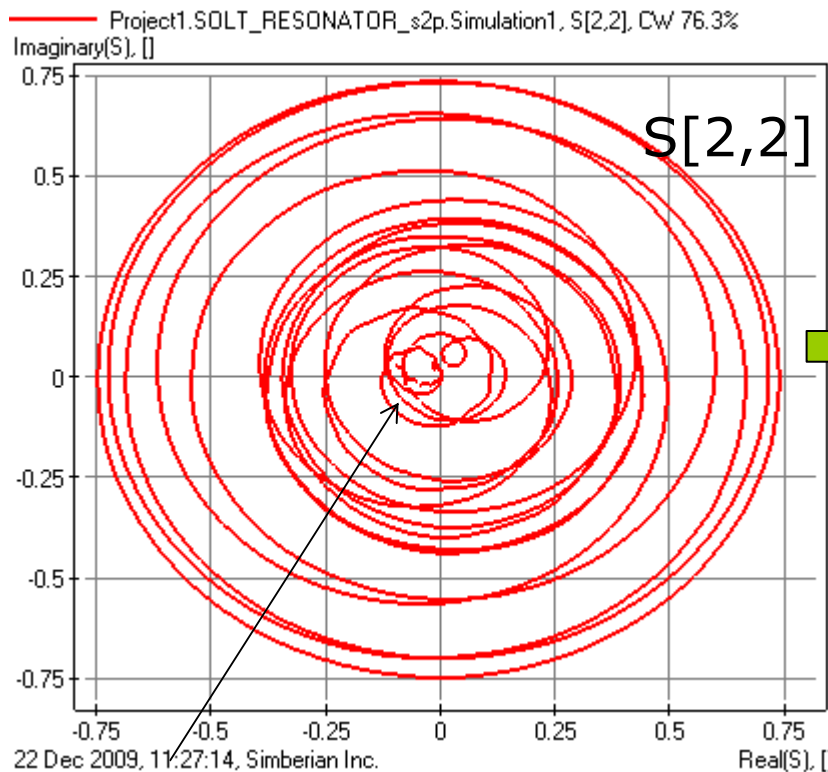


Touchstone model with DC and reduced number of frequency points  
or BB SPICE model can be produced from RCM

# Resonator (SOLT): Original S[2,2] and RCM

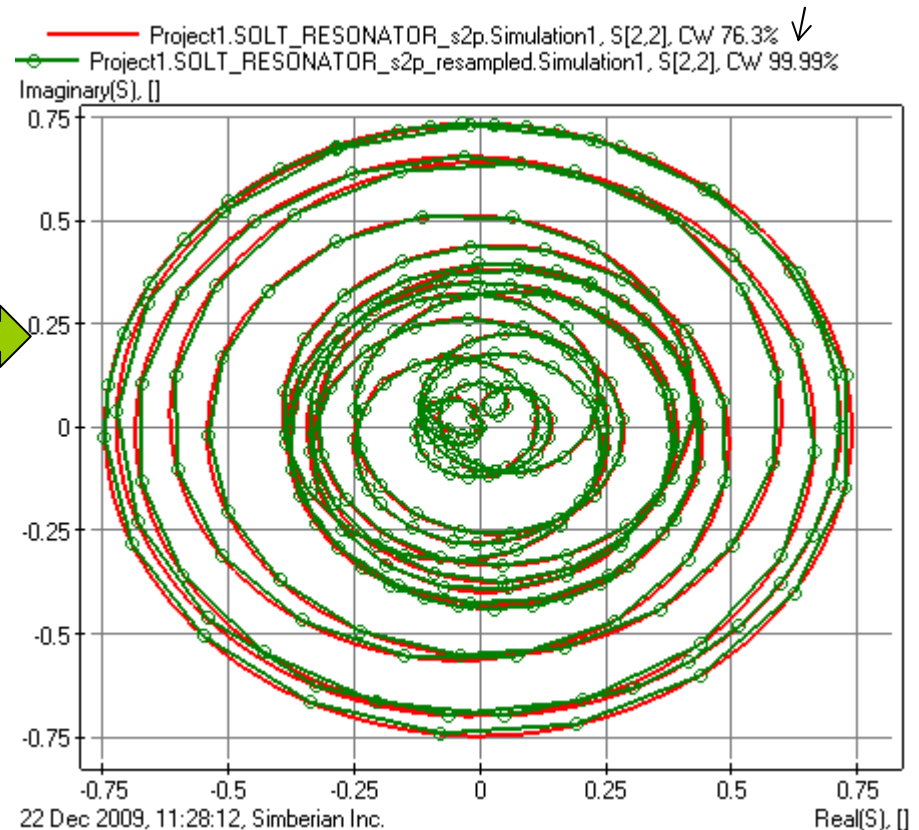
$$S_{i,j} = \text{Re}(S_{i,j}) + i \text{Im}(S_{i,j})$$

VNA Measurement: 3201 points  
starting from 300 KHz



Some noise at higher  
frequencies (minor issue)

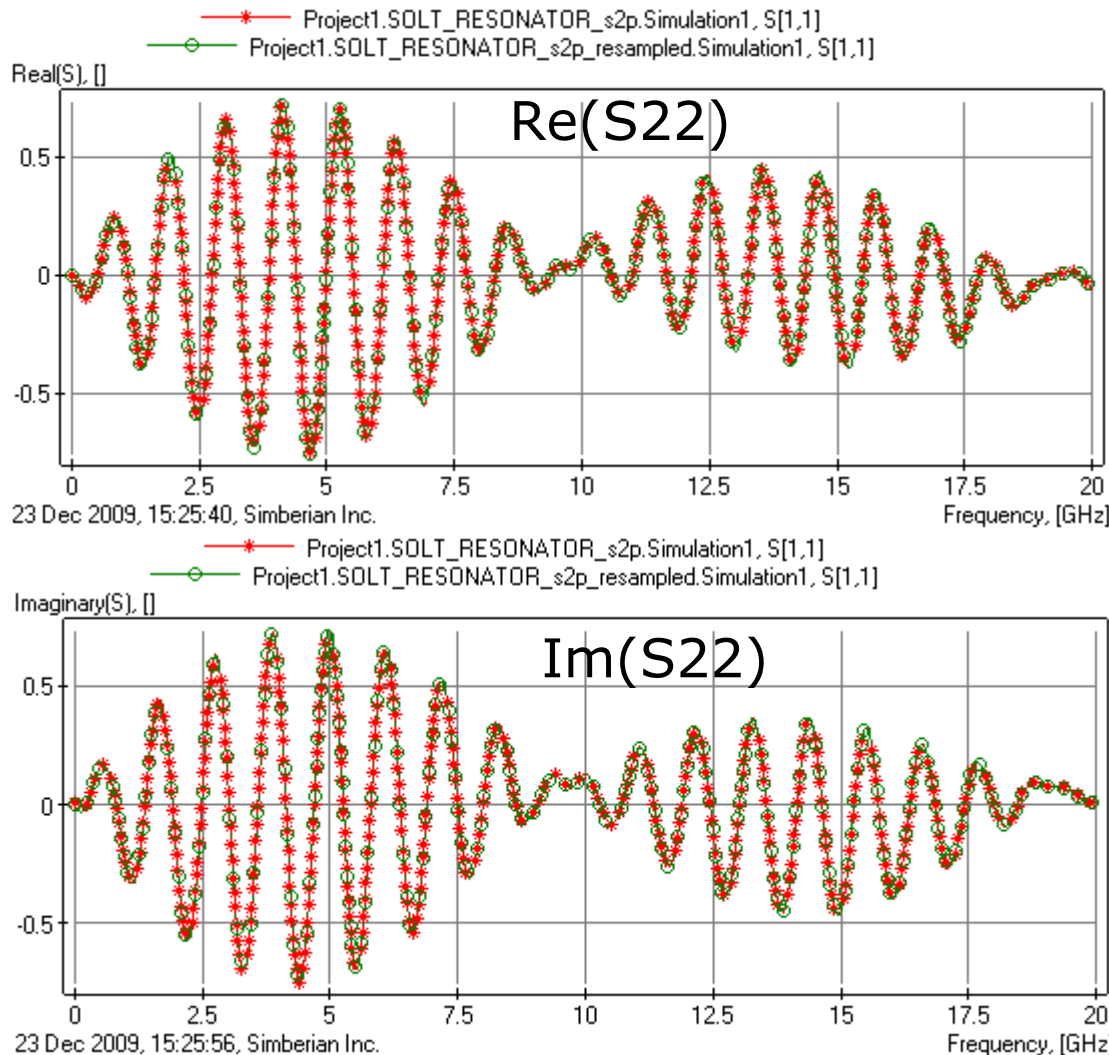
Re-sampled RCM: 485 points distributed  
adaptively starting from 0 Hz **CAUSAL!**



Red line – original VNA data  
Green line with circles – RCM

# Resonator (SOLT): Original S[2,2] and RCM

$$S_{i,j} = \text{Re}(S_{i,j}) + i \text{Im}(S_{i,j})$$



Stars – VNA data

Circles – RCM model

RCM: RMS Error 0.003,  
64 poles

RCM is practically  
indistinguishable and  
works in frequency as  
well as in time domain!

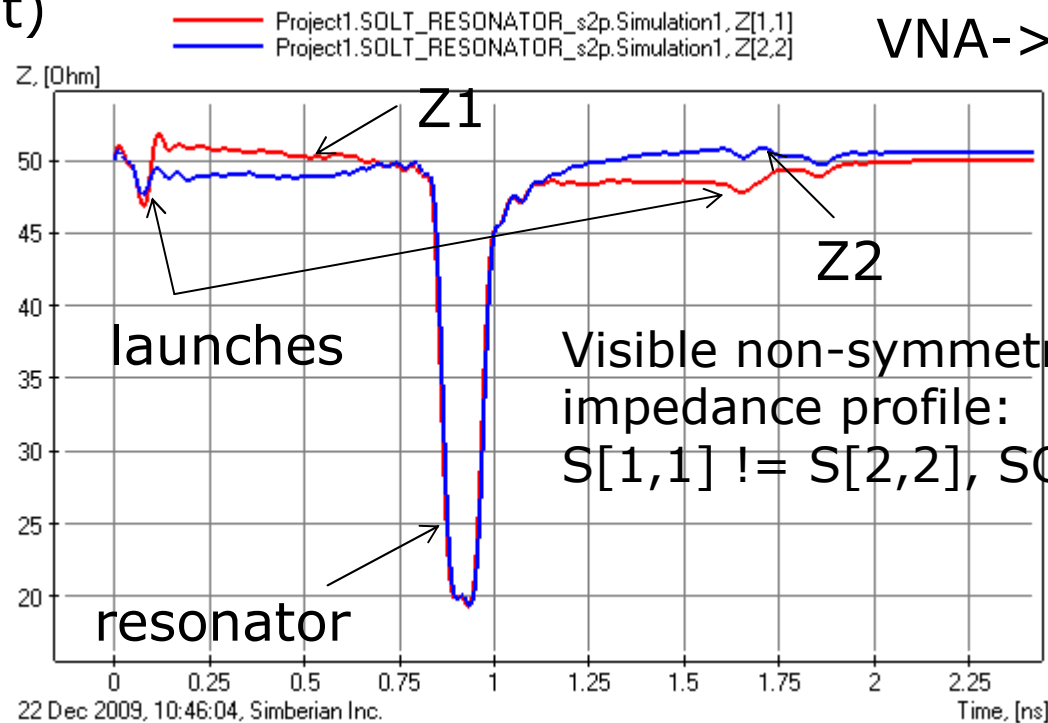
# Resonator TDR from RCM (SOLT)

Port 1



Port 2

$Z(t)$



*Effect of non-symmetry on TRL calibration is also the subject of our research*



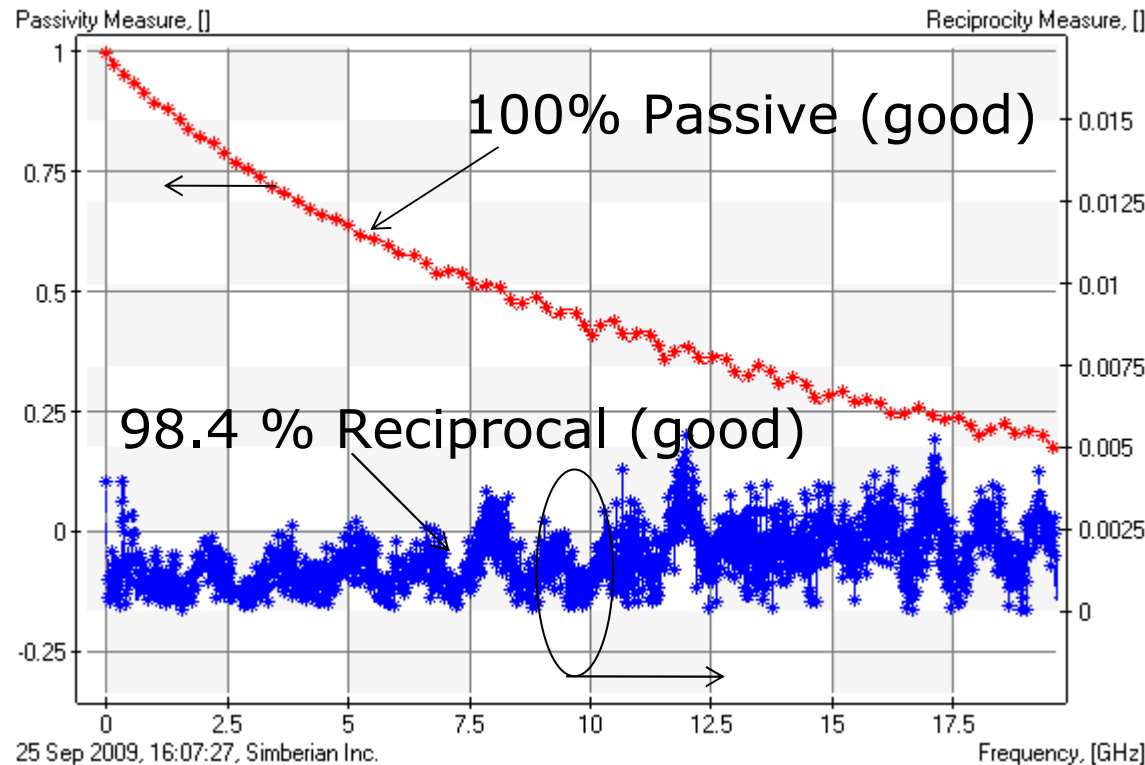
# S-parameters for a medium-reflection structure: Single controlled via, SOLT calibration

Port 1



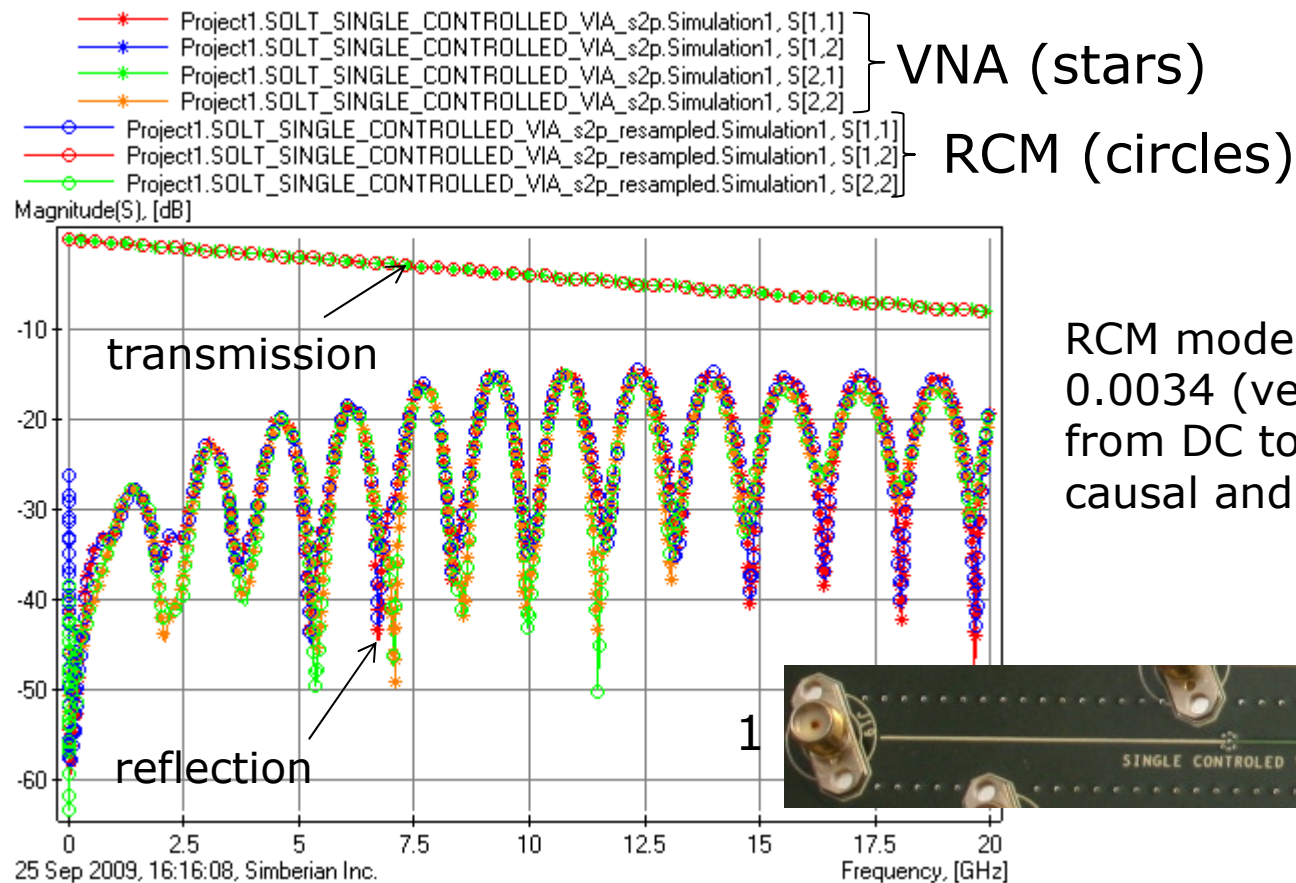
Port 2

Project1.SOLT\_SINGLE\_CONTROLLED\_VIA\_s2p.Simulation1  
MultiportParameters: S(Zo=50), Y, Z; ReciprocityQM=98.38%; SymmetryQM=72.05%; CausalityQM=9.5%



Causality problem,  
but it can be  
restored with RCM

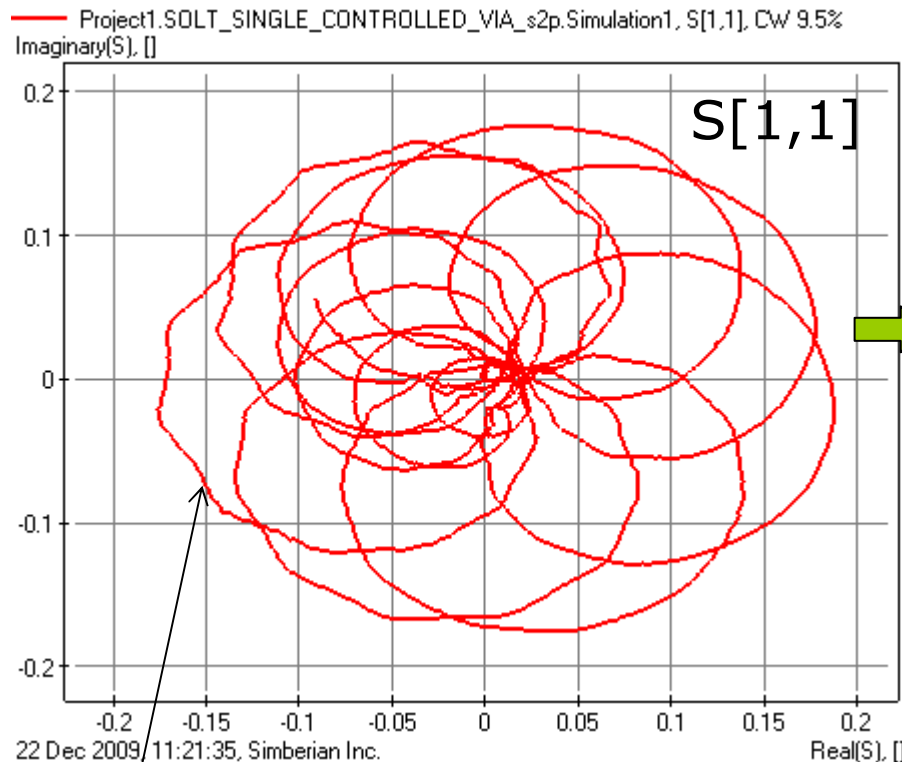
# Single controlled via (SOLT): Improving S-parameters with RCM



Touchstone model with DC and reduced number of frequency points or BB SPICE model can be produced from RCM

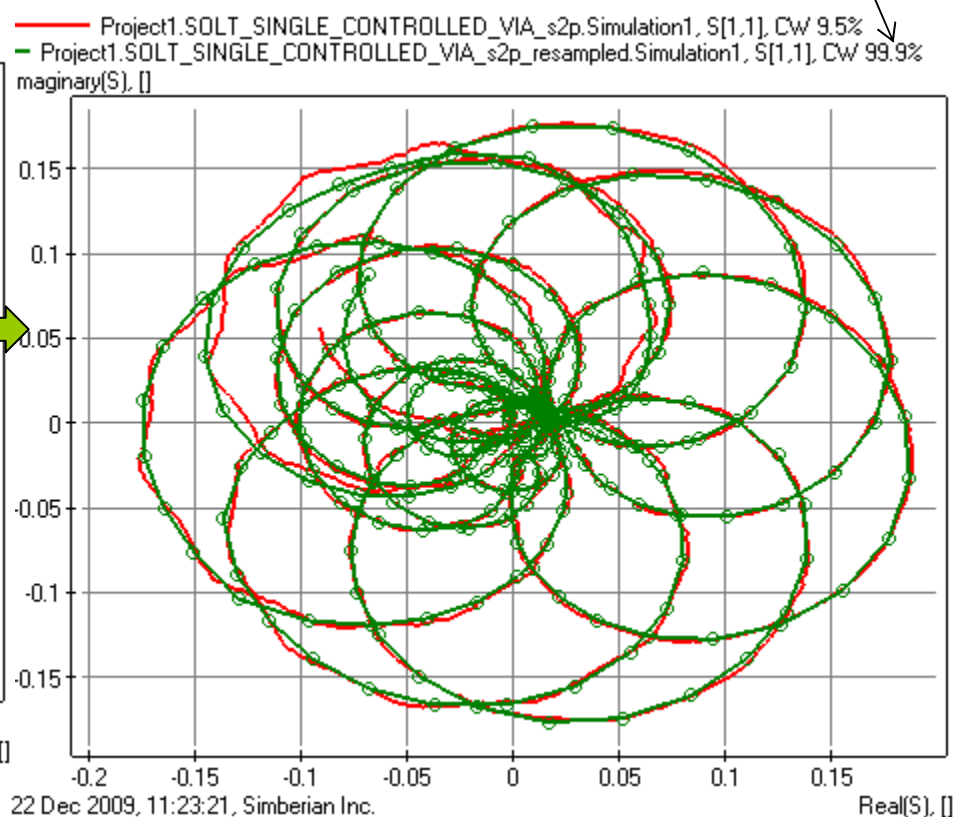
# Single controlled via (SOLT): Original S[1,1] and RCM

VNA Measurement: 3201 points  
starting from 300 KHz



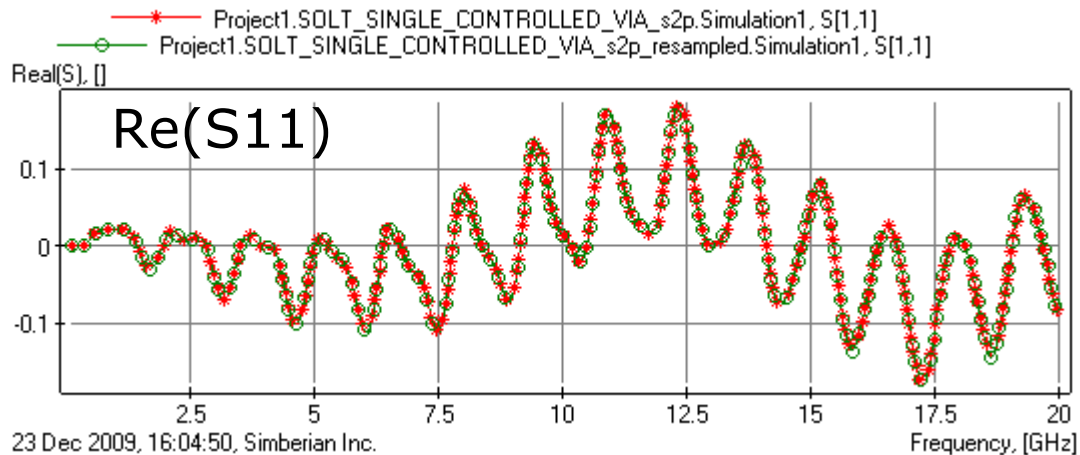
Visible noise and large segments  
with counter-clockwise rotation

Re-sampled RCM: 769 points distributed  
adaptively starting from 0 Hz **CAUSAL!**



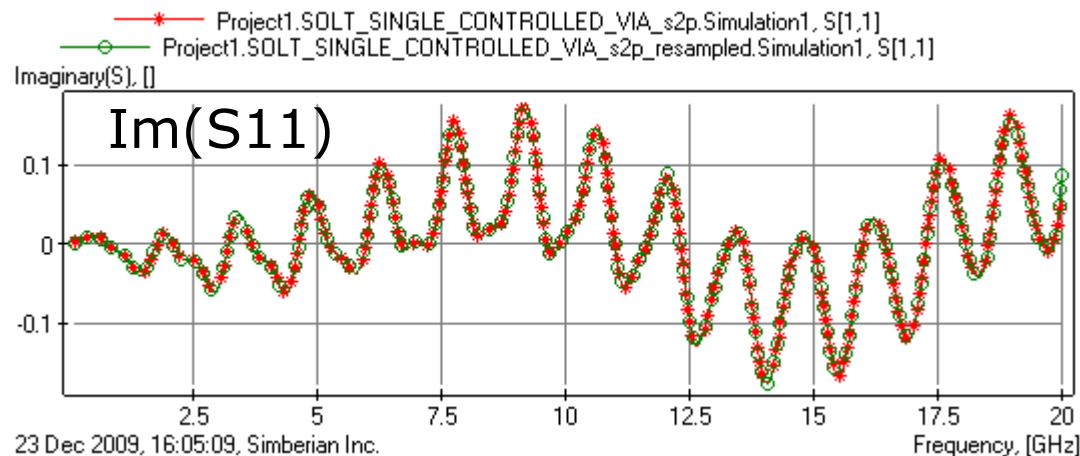
Red line – original VNA  
Green line with circles - RCM

# Single controlled via (SOLT): Original S[1,1] and RCM



Stars – VNA data  
Circles – RCM (corrected)

RCM: 46 poles,  
RMS Error 0.0034



Practically  
indistinguishable!

Age Group	Percentage
18-24	15%
25-34	25%
35-44	30%
45-54	20%
55-64	10%
65-74	5%
75-84	2%
85+	1%





# S-parameters from VNA: TRL-calibration data quality report

Project1.TRL_1_INCH_STRIPLINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9953%; ReciprocityQM=98.08%; SymmetryQM=51.48%; CausalityQM=15.8%
Project1.TRL_2_INCH_STRIPLINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9985%; ReciprocityQM=98.29%; SymmetryQM=57.93%; CausalityQM=20.3%
Project1.TRL_COUPLED_DIFFERENTIAL_MICROSTRIP_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9987%; ReciprocityQM=99.8%; SymmetryQM=64.5%; CausalityQM=0%
Project1.TRL_DIFFERENTIAL_VIA_TRANSITION_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9993%; ReciprocityQM=99.76%; SymmetryQM=44.31%; CausalityQM=0%
Project1.TRL_DUAL_DIFFERENTIAL_BEND_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9971%; ReciprocityQM=99.78%; SymmetryQM=41.22%; CausalityQM=0%
Project1.TRL_ISOLATED_DIFFERENTIAL_VIA_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9983%; ReciprocityQM=99.74%; SymmetryQM=7.4%; CausalityQM=0%
Project1.TRL_LOW_PASS_FILTER_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9987%; ReciprocityQM=98.83%; CausalityQM=39%
Project1.TRL_MULTI_TRANSITION_MICROSTRIP_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9986%; ReciprocityQM=98.82%; SymmetryQM=52.16%; CausalityQM=29.7%
Project1.TRL_OFFSET_RESONATOR_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9926%; ReciprocityQM=98.5%; SymmetryQM=7.3%; CausalityQM=26.1%
Project1.TRL_RESONATOR_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9916%; ReciprocityQM=98.51%; SymmetryQM=0%; CausalityQM=9.4%
Project1.TRL_ONE_INCH_25_OHM_LINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9588%; ReciprocityQM=97.88%; SymmetryQM=31.92%; CausalityQM=14.2%
Project1.TRL_ONE_INCH_80_OHM_LINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9946%; ReciprocityQM=97.98%; SymmetryQM=52.86%; CausalityQM=13.2%
Project1.TRL_SINGLE_CONTROLLED_VIA_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9524%; ReciprocityQM=97.48%; SymmetryQM=54.05%; CausalityQM=17.7%
Project1.TRL_SINGLE_DIFF_VIA_COUPLED_MICROSTRIP_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9981%; ReciprocityQM=99.71%; SymmetryQM=32.22%; CausalityQM=0%
Project1.TRL_THRU_WITH_MOLOEX_LAUNCH_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=0%; ReciprocityQM=97.14%; SymmetryQM=68.1%; CausalityQM=0%
Project1.TRL_TIGHTLY_COUPLED_MEANDERING_LINE_s2p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9974%; ReciprocityQM=98.62%; SymmetryQM=27.18%; CausalityQM=10%
Project1.TRL_TWO_DIFFERENTIAL_VIAS_COUPLED_MICROSTRIP_s4p.Simulation1	MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9992%; ReciprocityQM=99.72%; SymmetryQM=42.07%; CausalityQM=77.6%

Low causality measure  
due to noise in small  
reflection coefficients of  
SOLT calibrated data

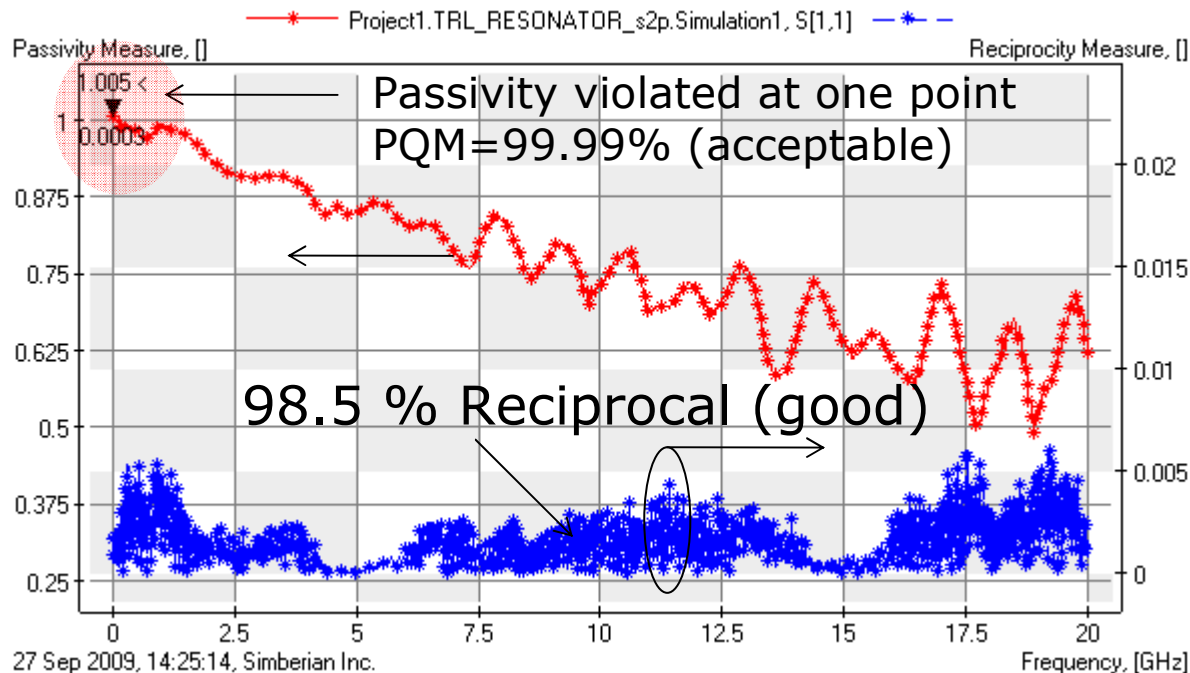
Passivity and  
Reciprocity are OK  
Non-symmetry is due  
to non-symmetry of the  
physical structures as in  
SOLT data

# S-parameters for a high-reflection structure: Resonator, TRL-calibration

TRL Reference Planes (750 mil from stubs)



Project1.TRL\_RESONATOR\_s2p.Simulation1  
MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9916%; ReciprocityQM=98.51%; SymmetryQM=0%; CausalityQM=9.4%



Causality dropped from 75.8% (SOLT) to 9.4% (TRL), but it can still be fixed with RCM

# Resonator (TRL): Causality problems

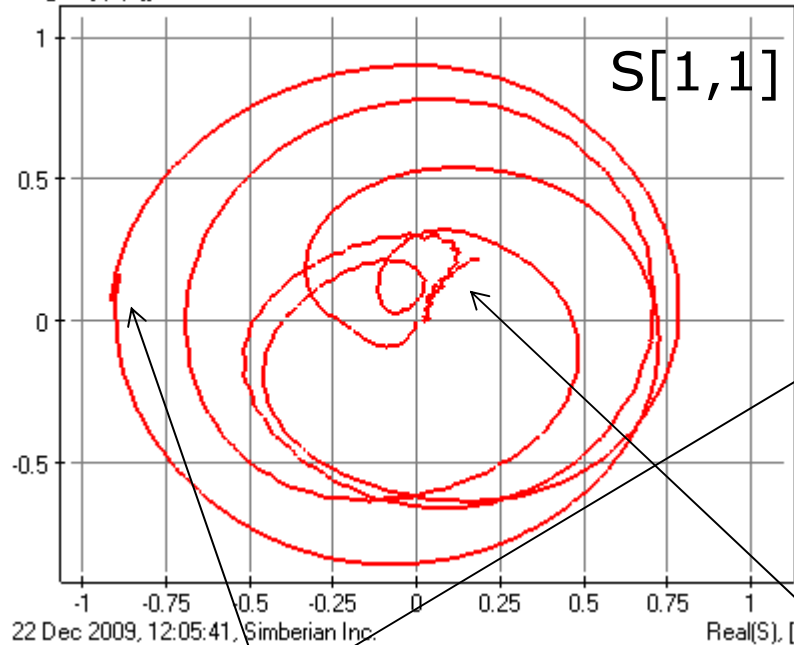
TRL Reference Planes (750 mil from stubs)

$S[1,2]$  is OK



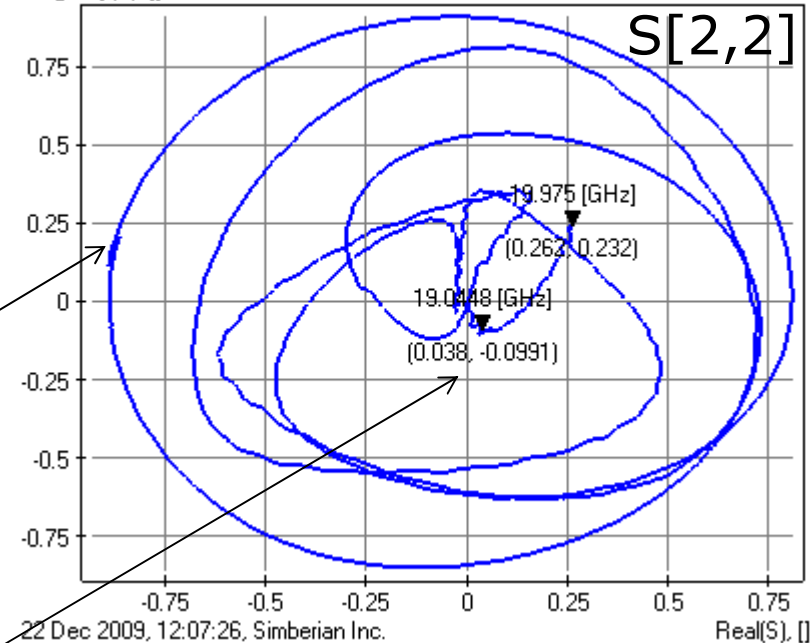
Worst causality

Project1.TRL\_RESONATOR\_s2p.Simulation1, S[1,1], CW 10.8%  
Imaginary(S), []



Glitches at 4.6 GHz

Project1.TRL\_RESONATOR\_s2p.Simulation1, S[2,2], CW 9.4%  
Imaginary(S), []

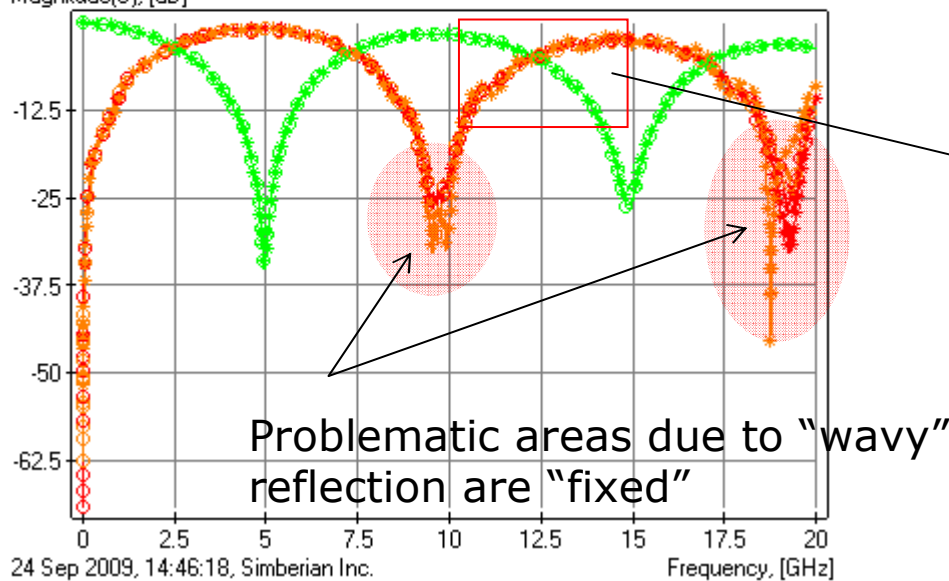
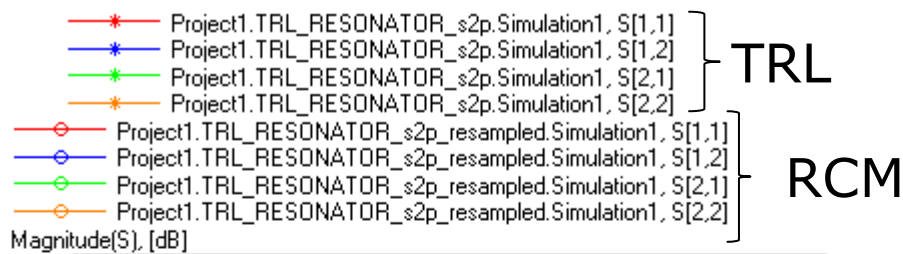


Noise and CCW rotation at low reflection

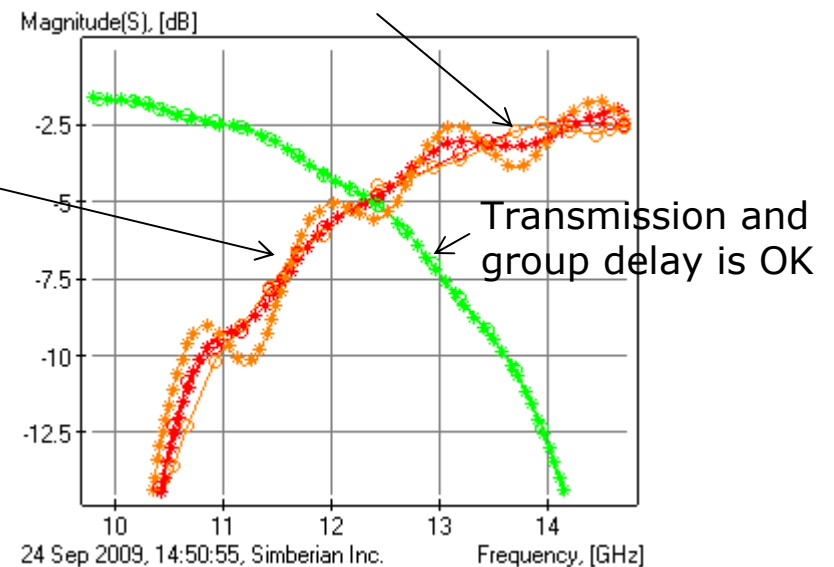
# Resonator (TRL): Improving S-parameters with RCM

RCM RMS Error is 0.07 (still OK)  
Passive from DC to infinity,  
causal and reciprocal

TRL Reference Planes  
(750 mil from stubs)

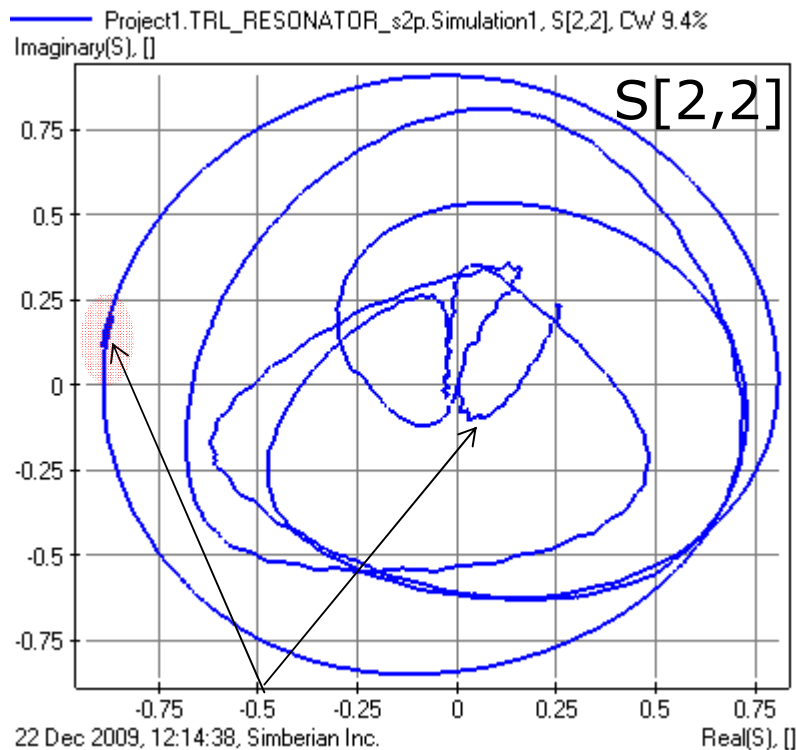


Problem is in the reflection parameters and RCM "fixes" it



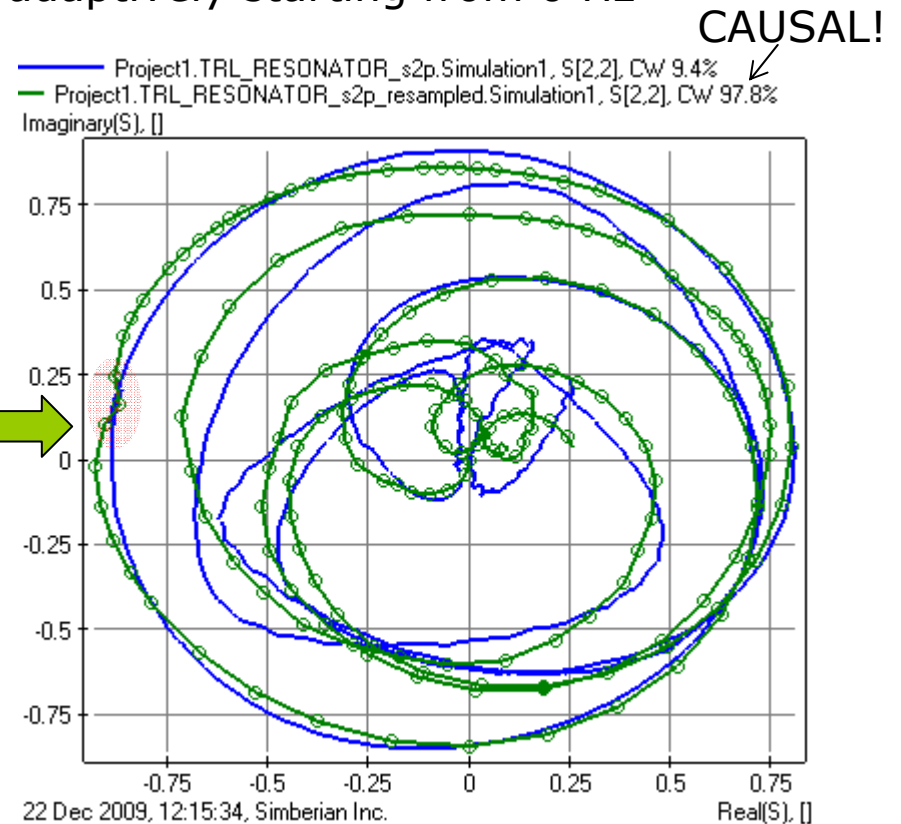
# Resonator (TRL): Original S[2,2] and RCM

VNA Measurement: 3201 points  
starting from 300 KHz



Glitch and noisy behavior at  
high frequencies

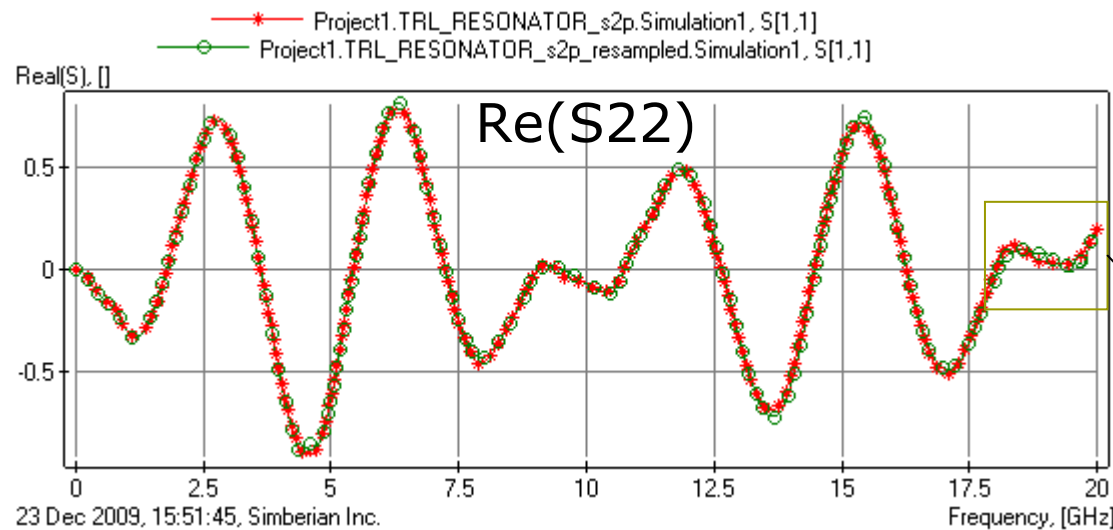
Re-sampled RCM: 310 points distributed  
adaptively starting from 0 Hz



Blue line – original TRL  
Green line with circles – RCM

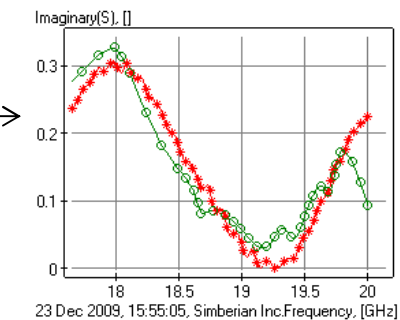
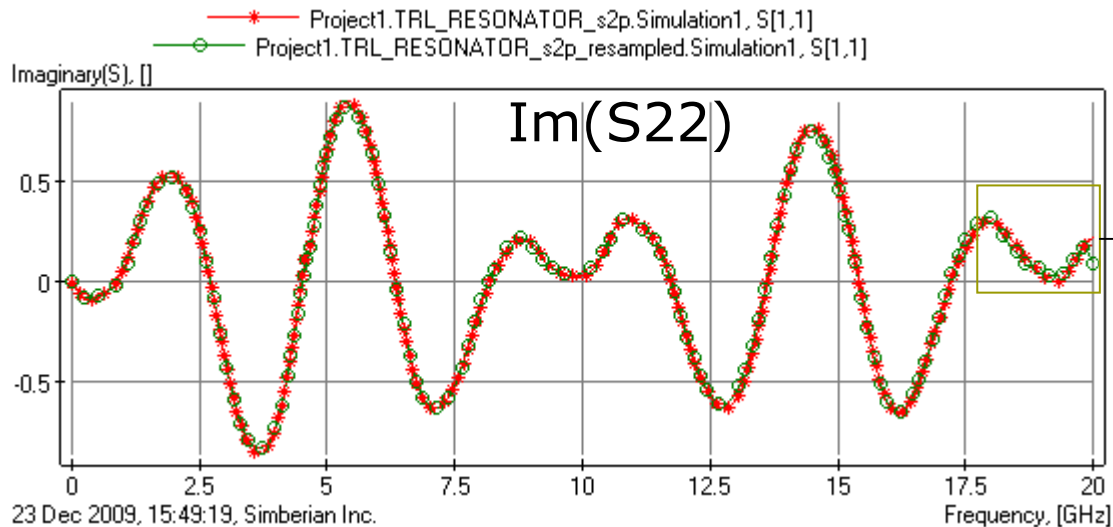
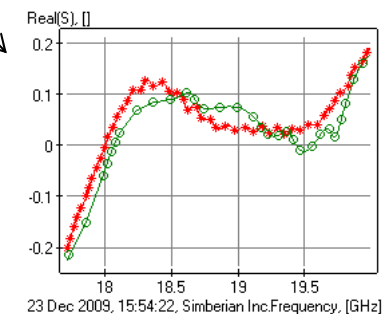


# Resonator (TRL): Original S[2,2] and RCM

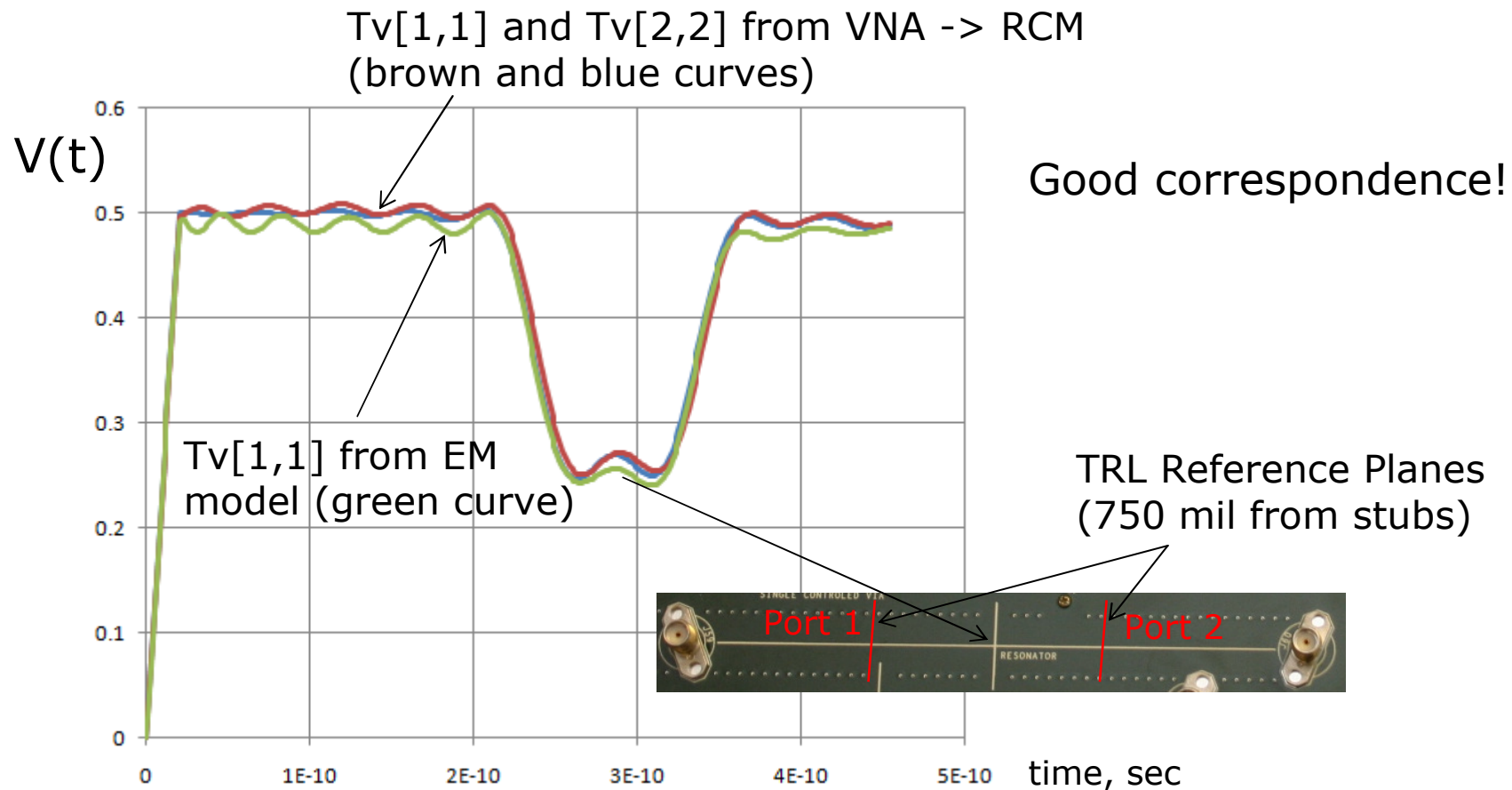


Stars – TRL data  
Circles – RCM model  
RMS Error 0.07, 50 poles

Problematic non-causal area  
is fitted as close as possible



# Resonator VNA vs. EM model (TRL)



**See more on modeling and measurements** at Y. Shlepnev, A. Neves, T. Dagostino, S. McMorro, *Measurement-Assisted Electromagnetic Extraction of Interconnect Parameters on Low-Cost FR-4 boards for 6-20 Gbps Applications*, DesignCon2009 – available at <http://www.simberian.com/AppNotes.php>

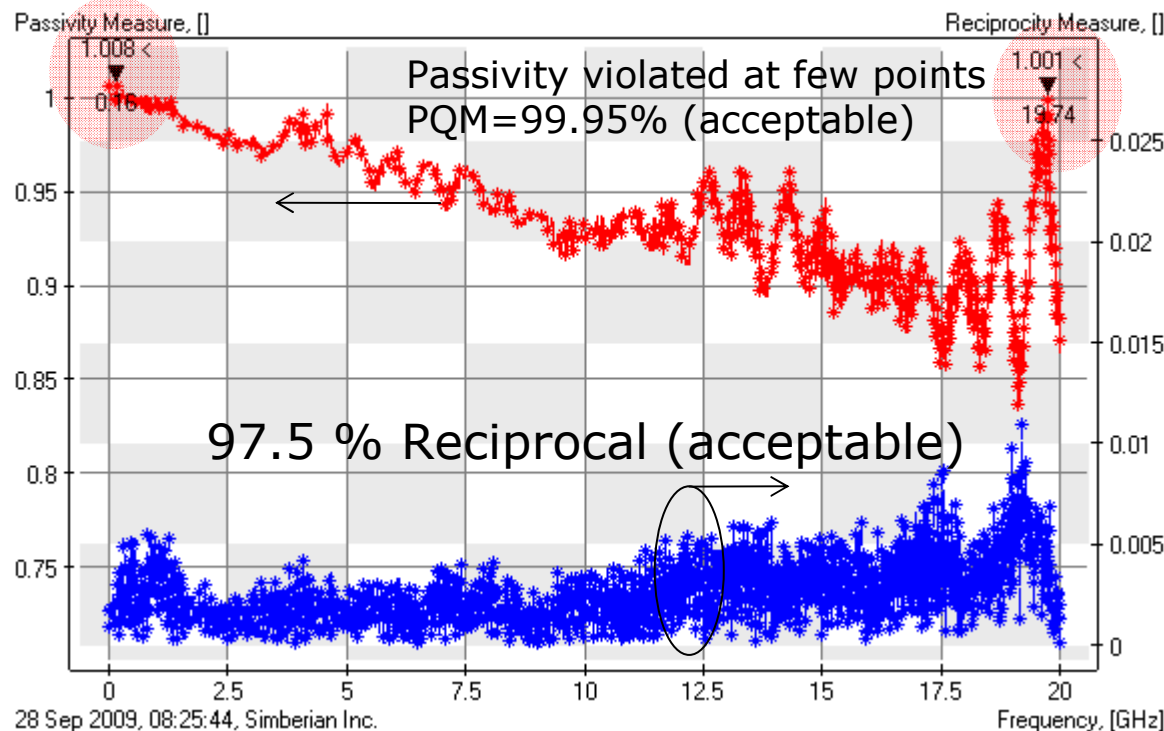
# S-parameters for a low-reflection structure: Single controlled via, TRL-calibration

TRL Reference Planes (250 mil from via)



Project1.TRL\_SINGLE\_CONTROLLED\_VIA\_s2p.Simulation1

MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9524%; ReciprocityQM=97.48%; SymmetryQM=54.05%; CausalityQM=17.7%



Causality is 17.7%, that is even slightly better than the original SOLT 9.5%

Passivity and reciprocity worsened comparing to SOLT, but still OK

28 Sep 2009, 08:25:44, Simberian Inc.

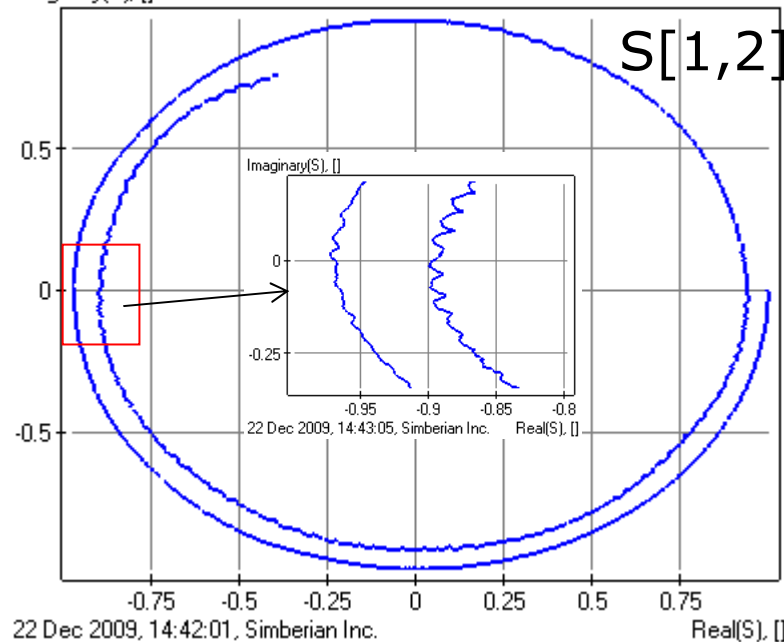
# Single controlled via (TRL): Causality problems both in transmission and reflection

TRL Reference Planes (250 mil from stubs)

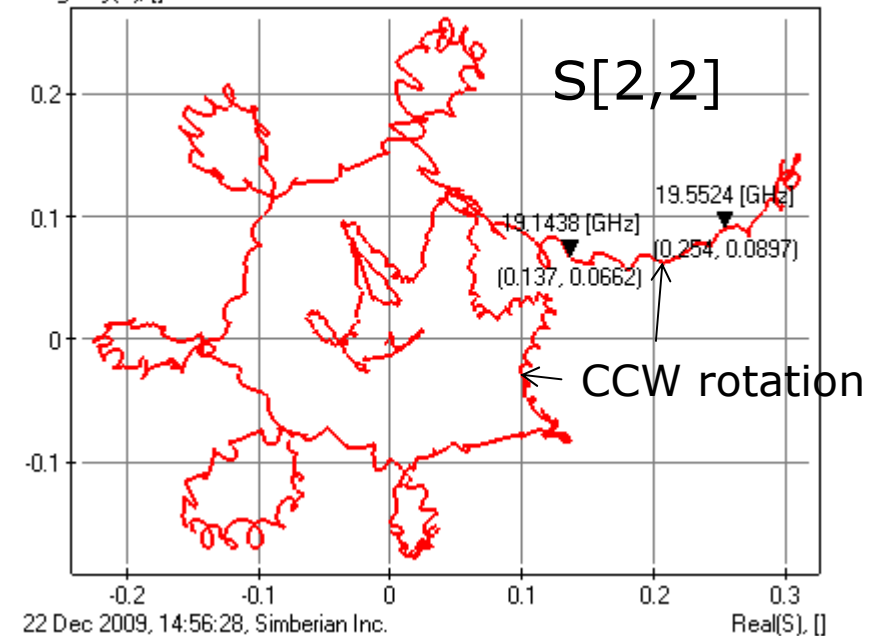


Some problems both in the transmission and reflection parameters (can be fixed):

Project1.TRL\_SINGLE\_CONTROLLED\_VIA\_s2p.Simulation1, S[1,2], CW 24.8%  
Imaginary(S), []



Project1.TRL\_SINGLE\_CONTROLLED\_VIA\_s2p.Simulation1, S[2,2], CW 46.4%  
Imaginary(S), []



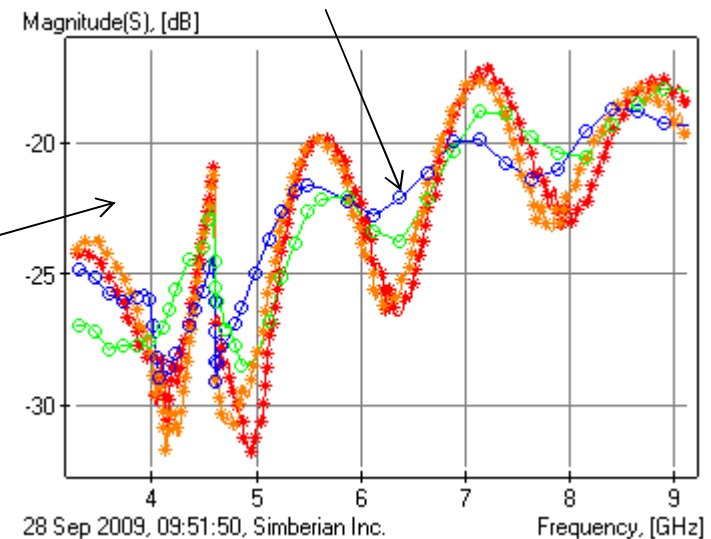
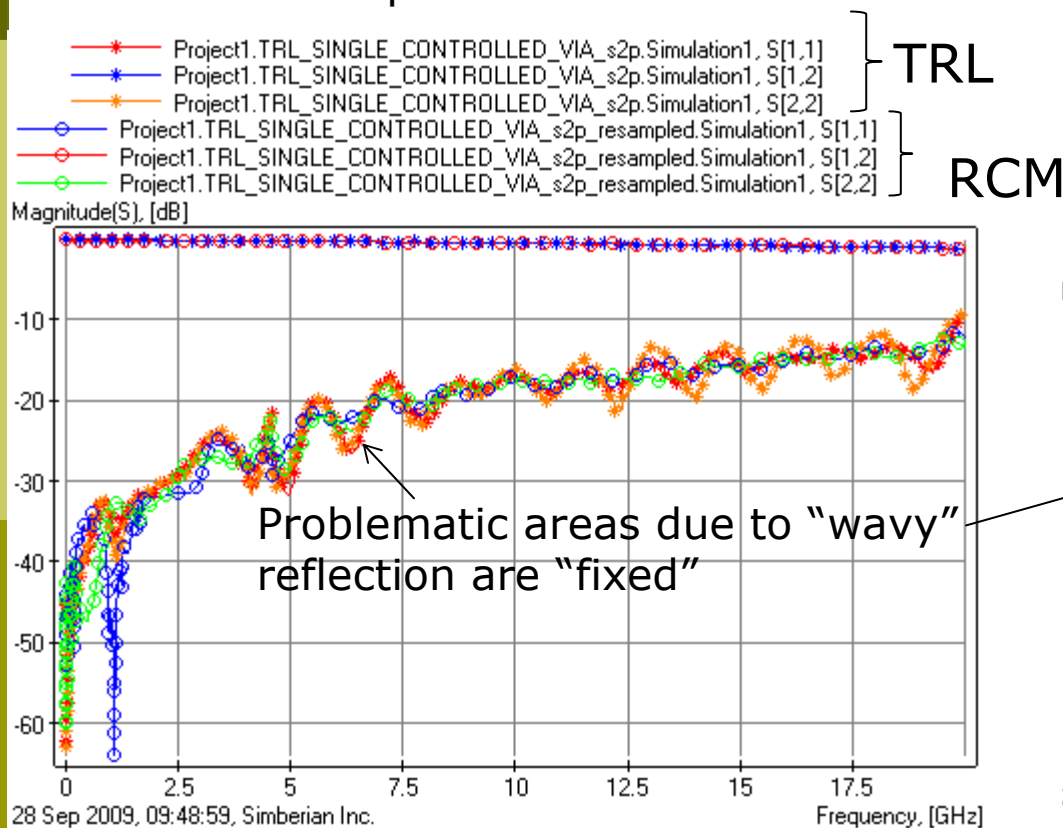
# Single controlled via (TRL): Improving S-parameters with RCM

RCM RMS Error is 0.045 (still OK)  
Passive from DC to infinity,  
Causal and reciprocal



Transmission and  
group delay is OK

Problem is in the reflection  
parameters and RCM "fixes" it  
with the best possible fit

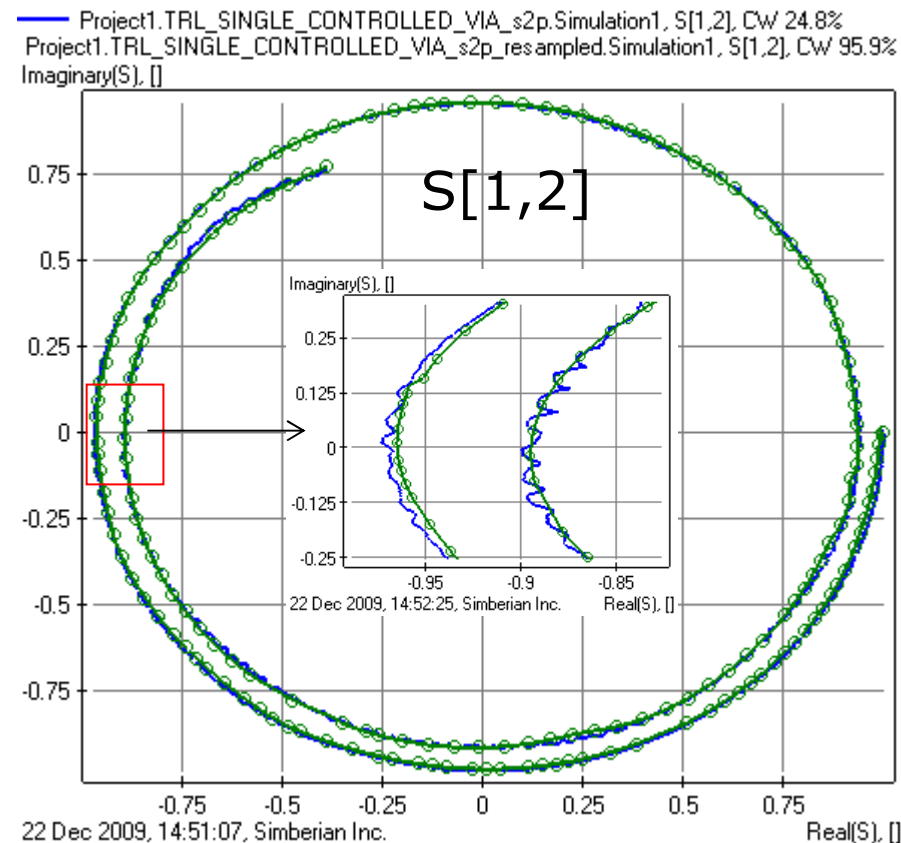




# Single controlled via (TRL): Original S[1,2] and RCM

VNA Measurement: 3201 points  
starting from 300 KHz

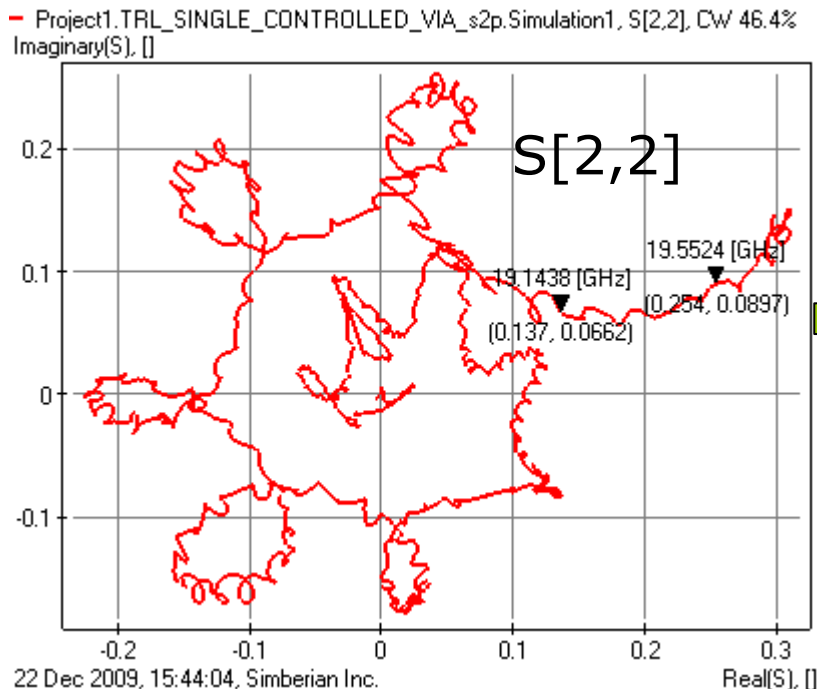
Re-sampled RCM: 633 points distributed  
adaptively starting from 0 Hz



Very noisy data is  
corrected with RCM!

# Single controlled via (TRL): Original S[2,2] and RCM

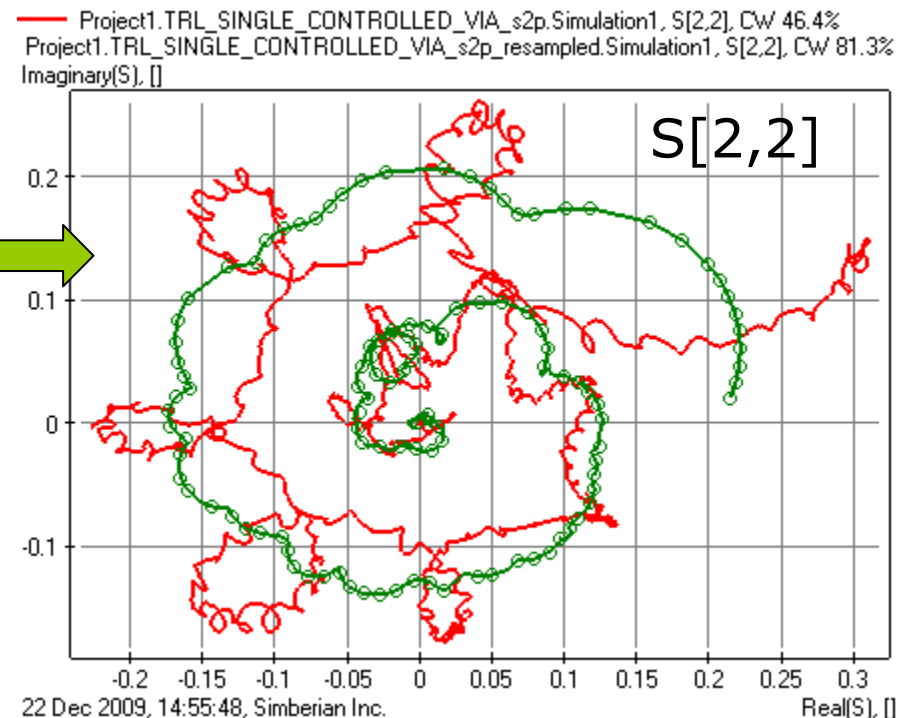
VNA Measurement: 3201 points  
starting from 300 KHz



Very noisy non-causal data with  
wrong rotation!

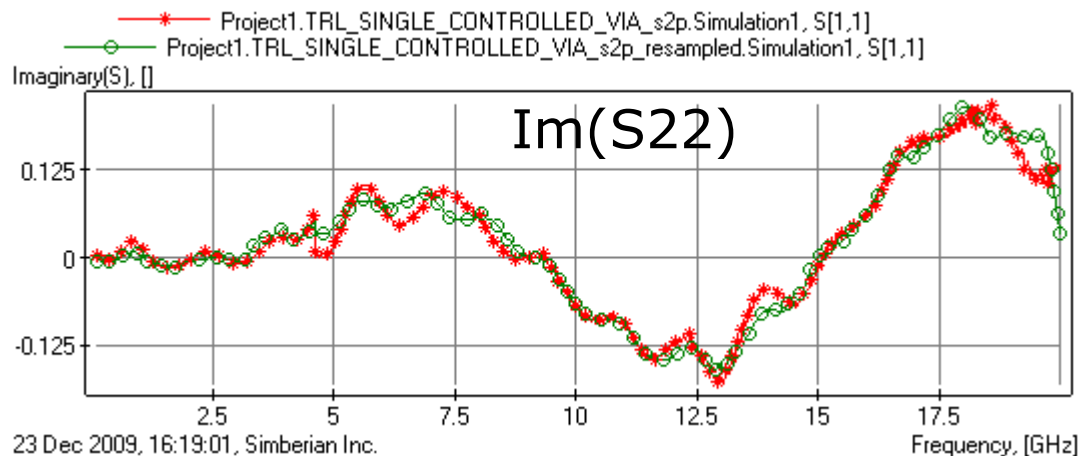
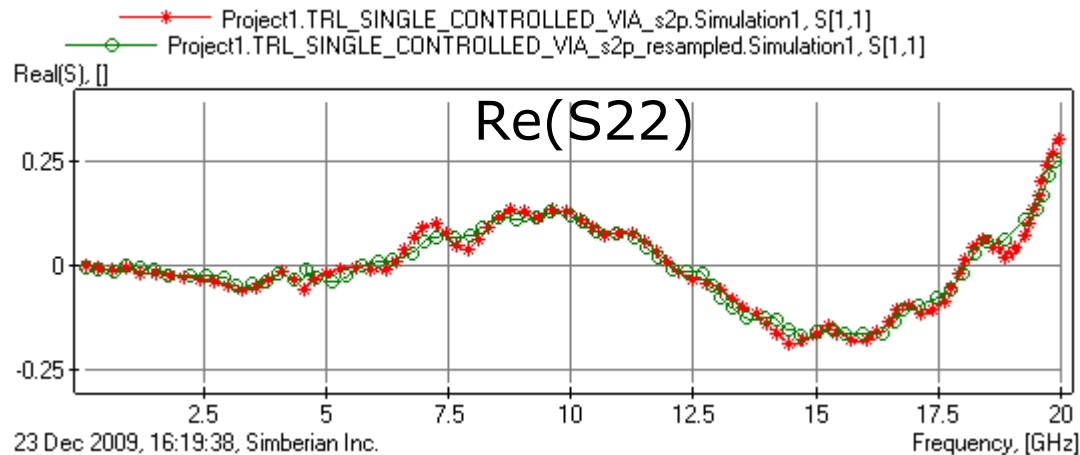
Re-sampled RCM: 633 points distributed  
adaptively starting from 0 Hz

Does not match well but CAUSAL ☺



Red line – original TRL data  
Green line with circles - RCM

# Single controlled via (TRL): Original S[2,2] and RCM



Stars – original TRL data  
Circles – RCM model

RMS Error 0.045,  
44 poles

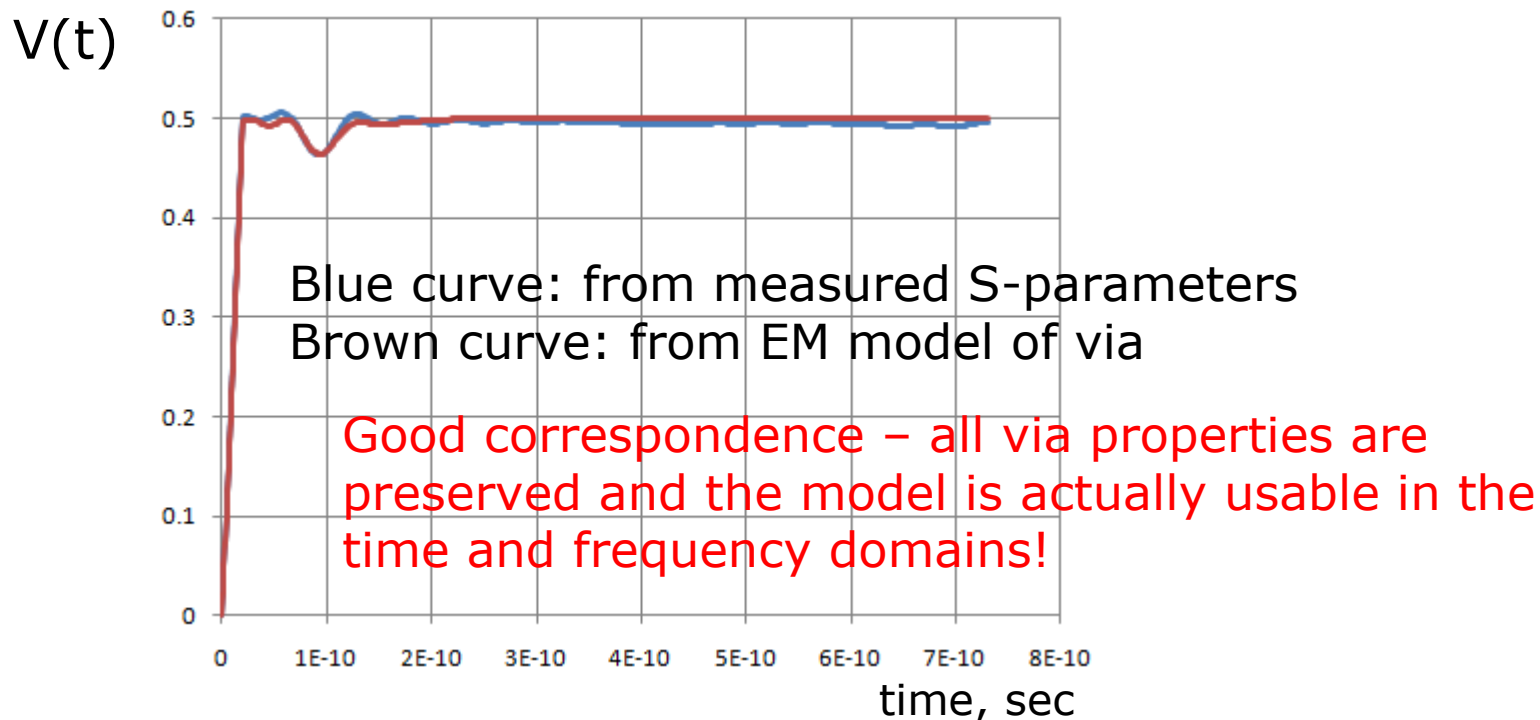
Problematic non-causal areas  
are fitted as close as possible

Does the corrected data  
contain information  
about the via?

# Single controlled via TDR from RCM (TRL)

Pure via in a t-line:  
no connector and launch  
discontinuities

TRL Reference Planes (250 mil from stubs)



# Conclusion

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- ❑ Always verify reciprocity, passivity and causality of interconnect component models before use
  - Measured models may be not acceptable for the analysis
  - Electromagnetic models may have violations too
- ❑ Distinguish minor “fixable” violations with acceptable accuracy degradation from severe violations
- ❑ Build macro-models with controllable accuracy to “improve” tabulated models and to correct minor violations of passivity and causality
- ❑ Verify macro-model both in frequency and time domains for consistency of the results

# Please visit us

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- ❑ Simberian Inc.
  - Booth #915 – Simbeor software and PLRD-1 board
  - [www.simberian.com](http://www.simberian.com)
- ❑ Teraspeed Consulting Group
  - [www.teraspeed.com](http://www.teraspeed.com)

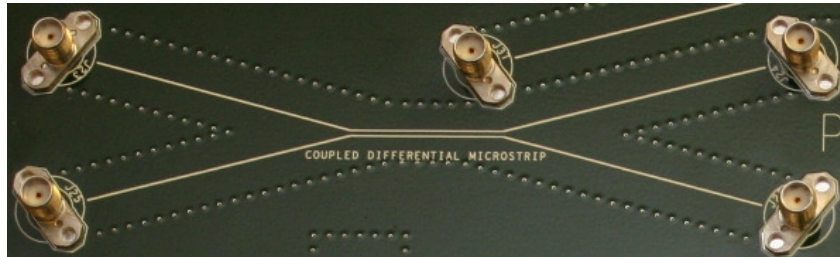


# Backup slides

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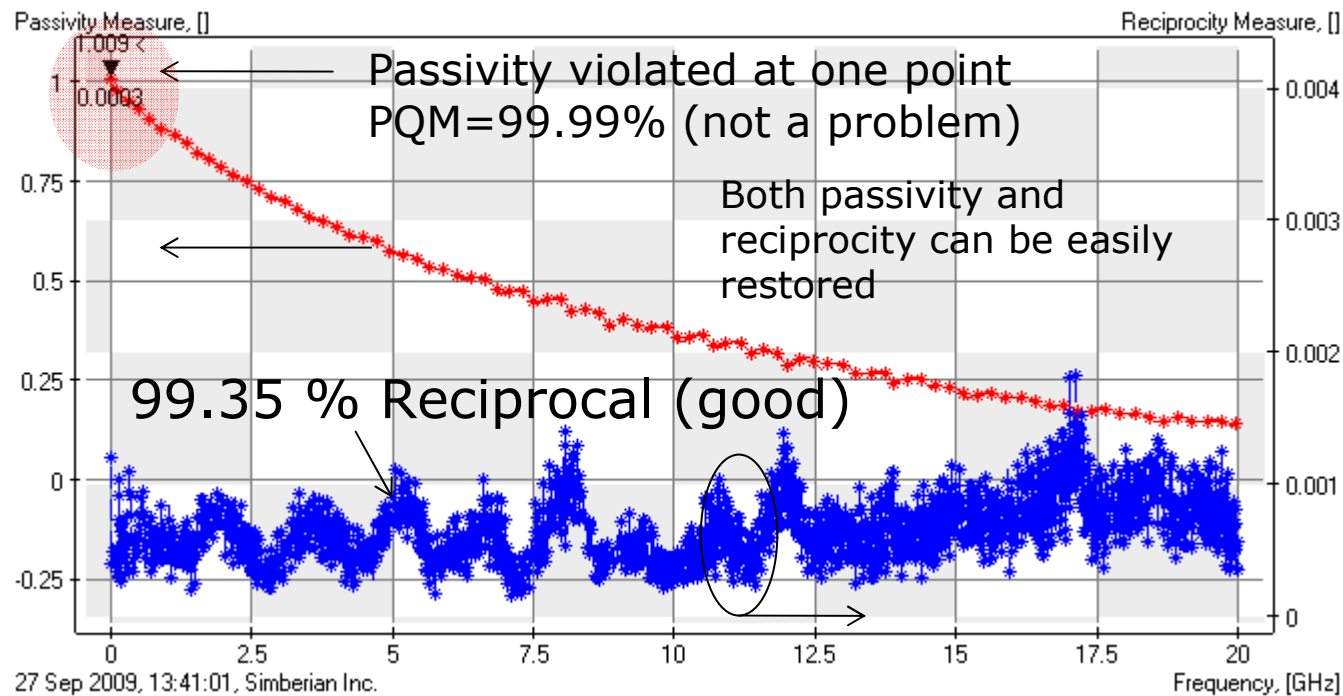
- SOLT-calibrated differential line segment
- TRL-calibrated differential line segment

# S-parameters from a low-reflective structure: Coupled differential micro-strip, SOLT



Causality, can be restored with RCM

Project1.SOLT\_COUPLED\_DIFFERENTIAL\_MICROSTRIP\_s4p.Simulation1  
MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9967%; ReciprocityQM=99.35%; SymmetryQM=73.76%; CausalityQM=6.9%

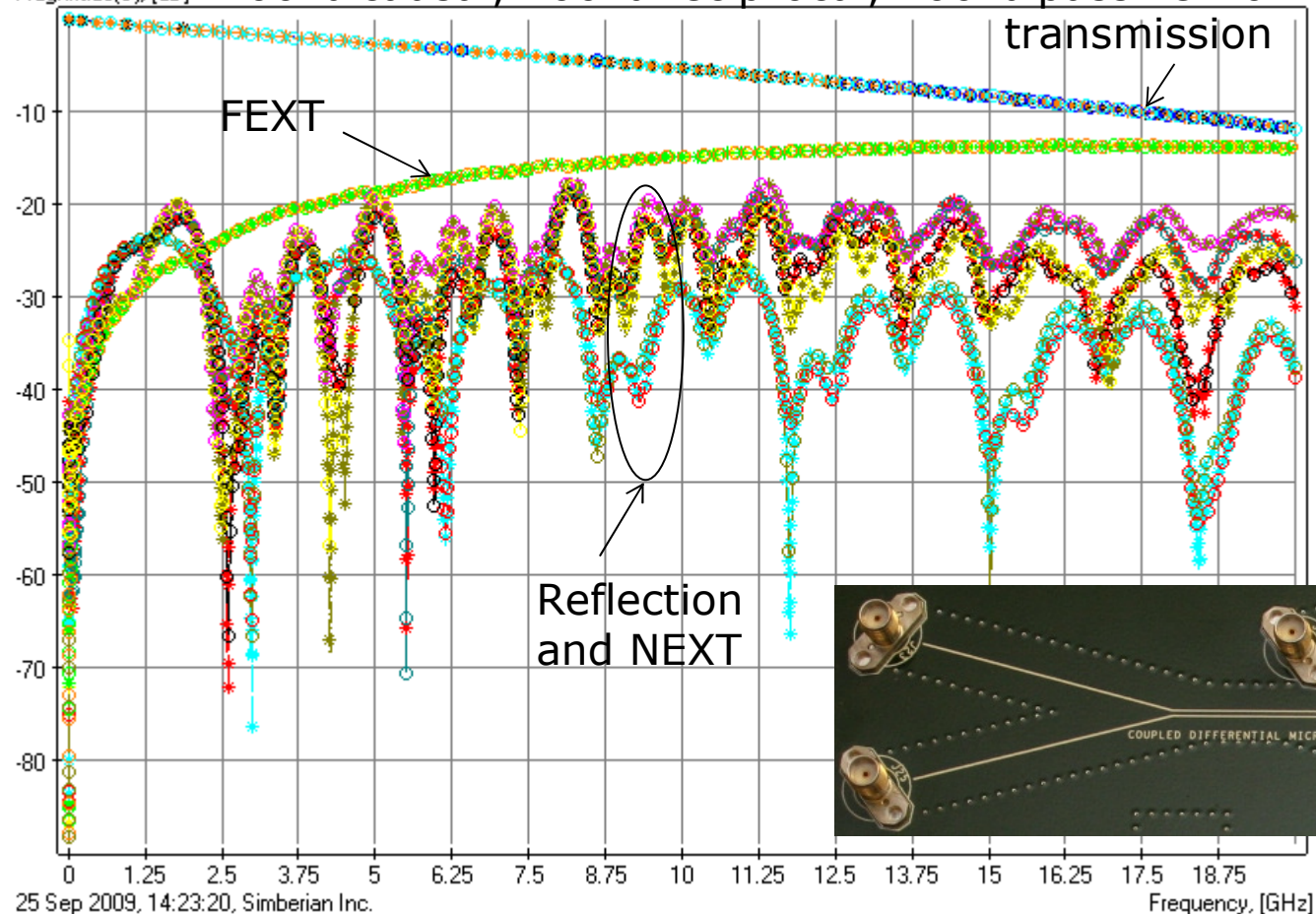


# Coupled differential micro-strip (SOLT): Improving S-parameters with RCM

Stars - VNA

Circles – RCM with 27 to 165 poles per element, RMS Error 0.0024,

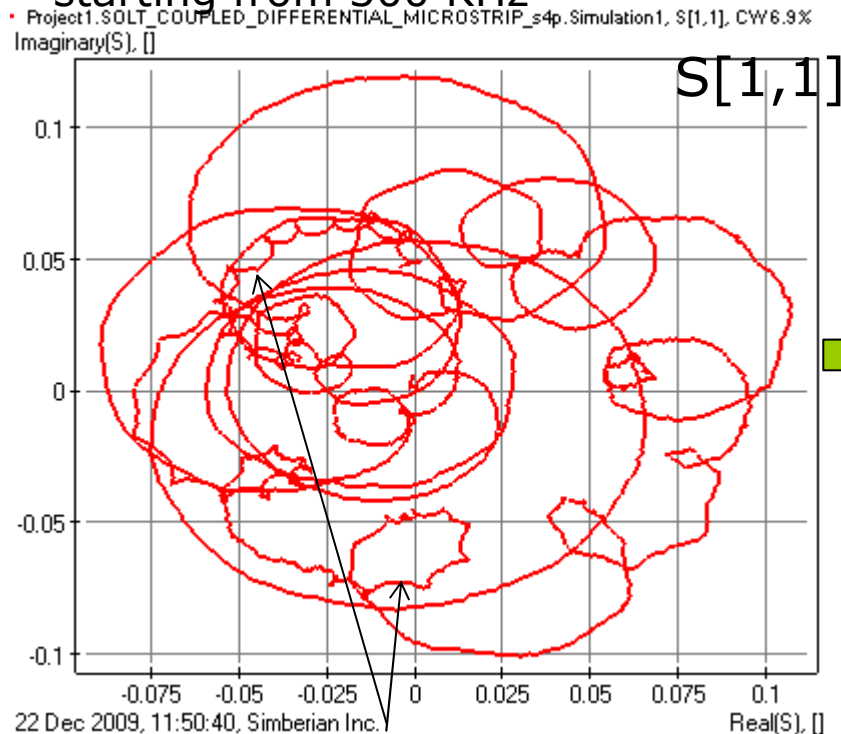
100% causal, 100% reciprocal, 100% passive from DC to infinity



25 Sep 2009, 14:23:20, Simberian Inc.

# Coupled differential micro-strip (SOLT): Original and improved $S[1,1]$

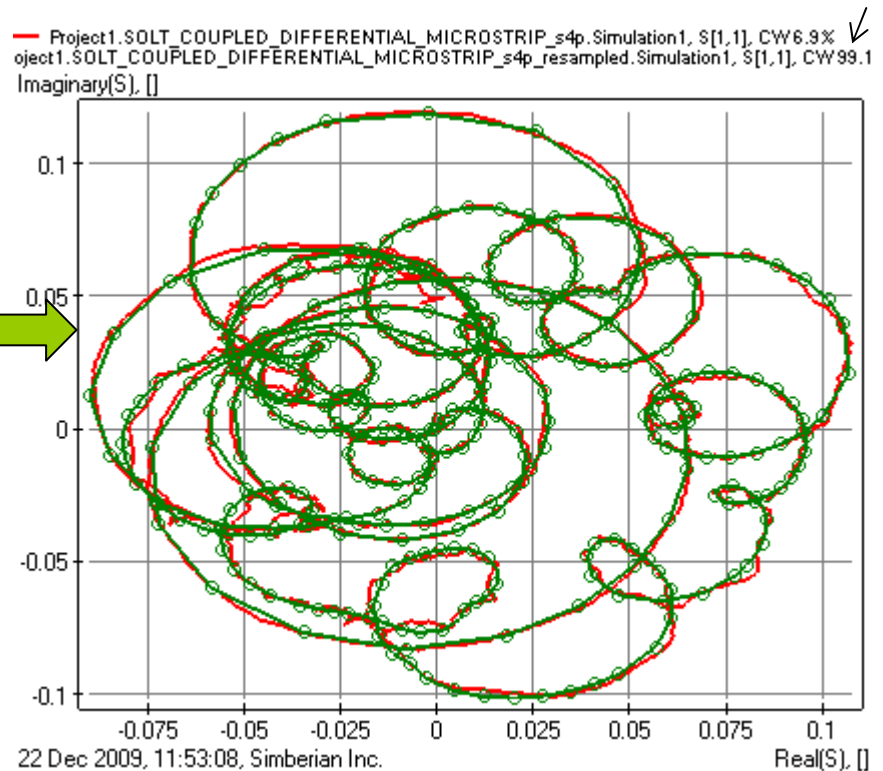
VNA Measurement: 3201 points  
starting from 300 KHz



Visible noise and counter-clockwise rotations

Reflections and NEXT are worst from the causality point of view due to smallness, but repairable with RCM

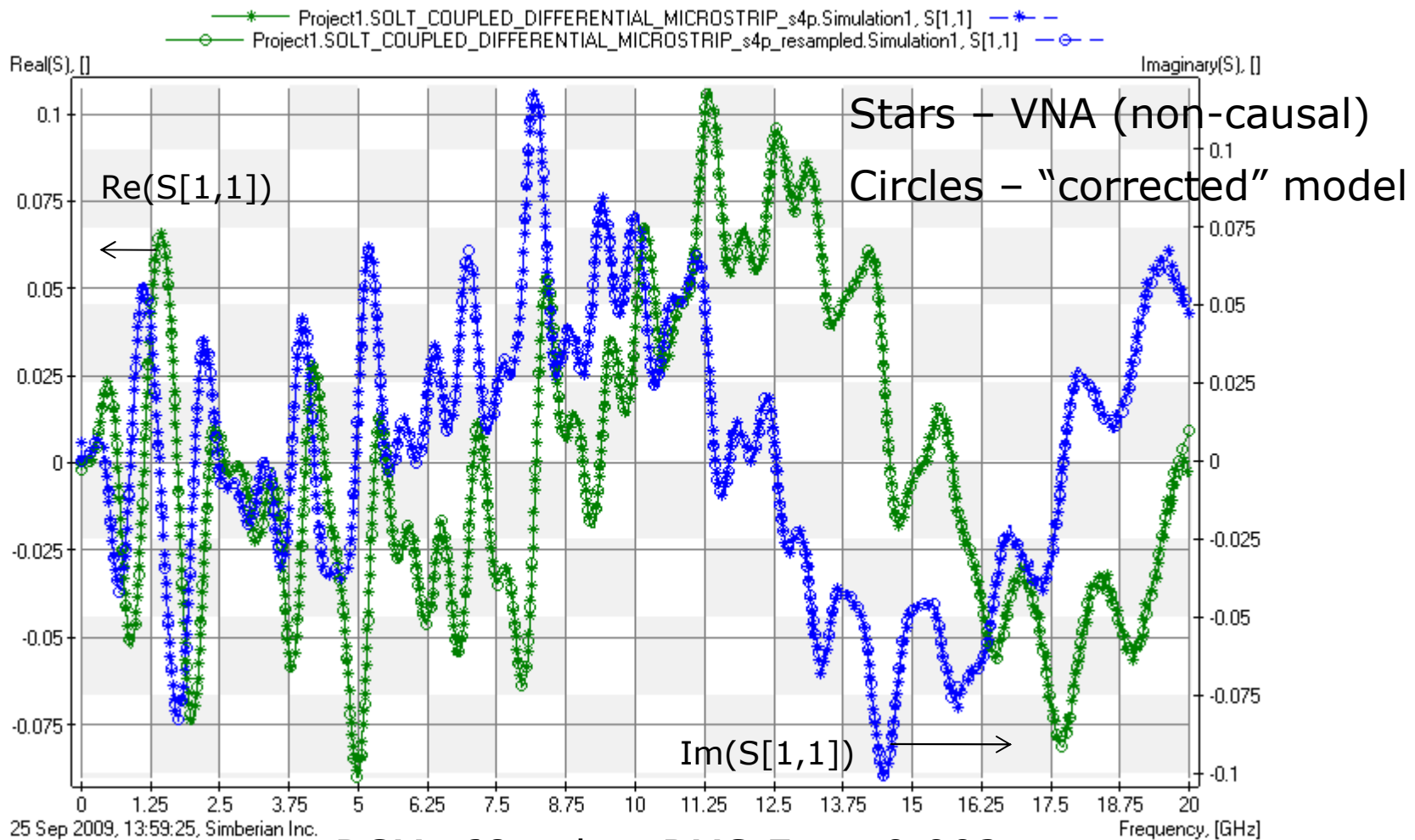
Re-sampled RCM: 687 points distributed adaptively starting from 0 Hz **CAUSAL!**



Red line – original

Green line with circles - corrected

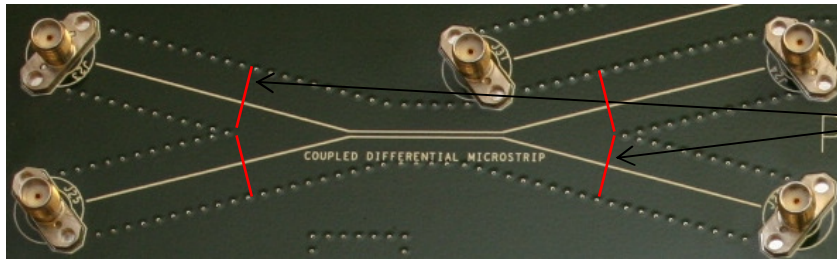
# Coupled differential micro-strip (SOLT): Original and improved S[1,1]



RCM: 68 poles, RMS Error 0.002



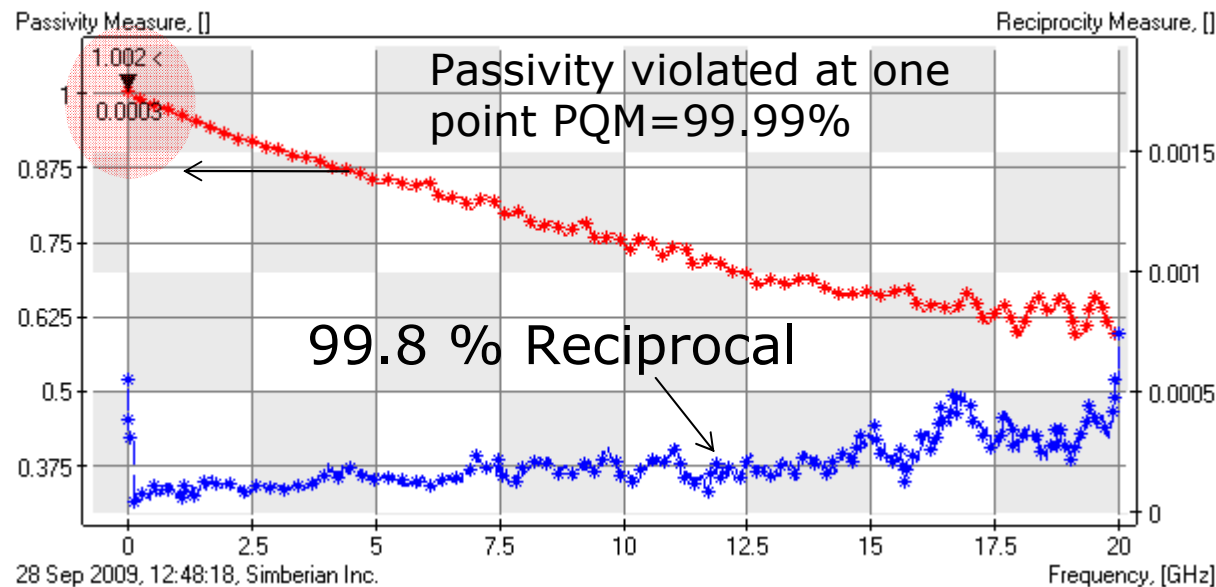
# S-parameters for a low-reflection structure: Coupled differential micro-strip, TRL-calibration



TRL Reference Planes (250 mil from differential section)

Project1.TRL\_COUPLED\_DIFFERENTIAL\_MICROSTRIP\_s4p.Simulation1

MultiportParameters: S(Zo=50), Y, Z; PassivityQM=99.9987%; ReciprocityQM=99.8%; SymmetryQM=64.5%; CausalityQM=0%

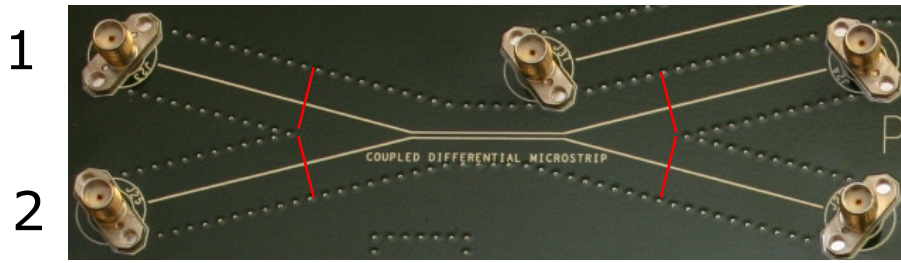


Big problems with causality in reflection parameters

Passivity and reciprocity are practically same as in SOLT



# Coupled differential micro-strip (TRL): Causality problems in reflection



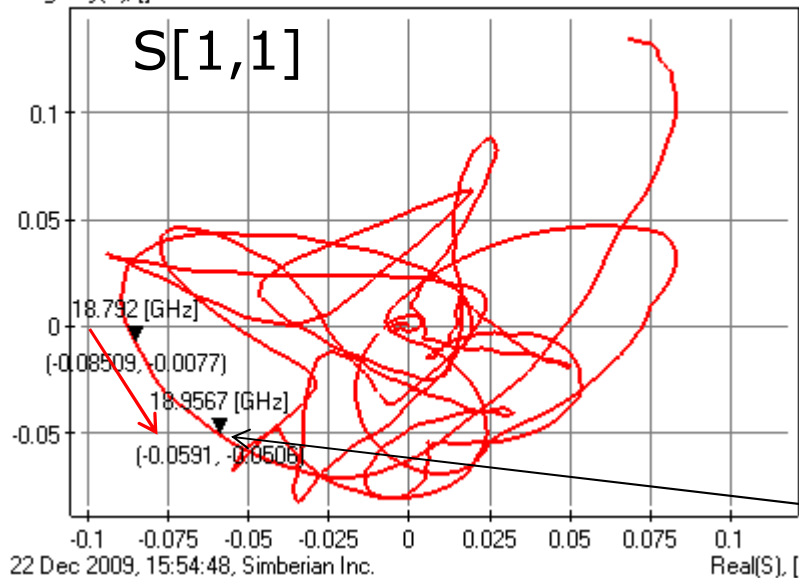
3

Transmission  
parameters are OK –  
minor noise problems

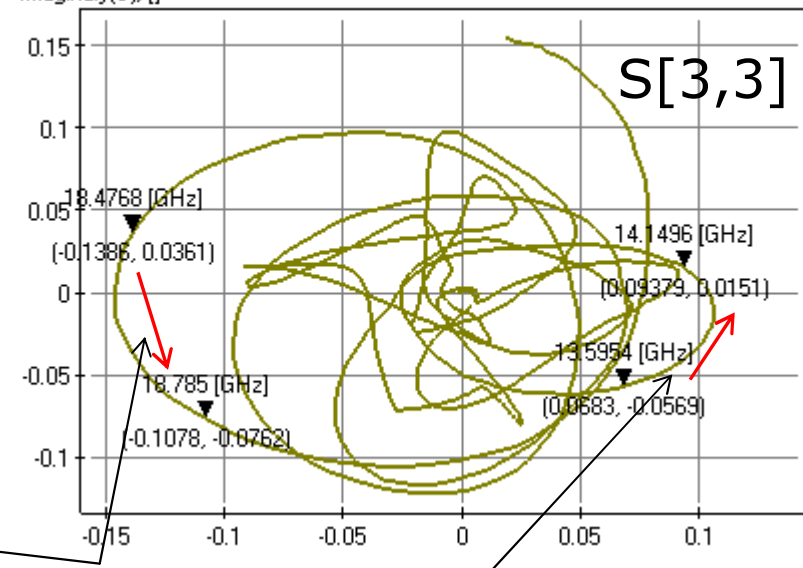
4

Severe problems in the reflection parameters (cannot be corrected):

• Project1.TRL\_COUPLED\_DIFFERENTIAL\_MICROSTRIP\_s4p.Simulation1, S[1,1], CW7.3%  
Imaginary(S), []



— Project1.TRL\_COUPLED\_DIFFERENTIAL\_MICROSTRIP\_s4p.Simulation1, S[3,3], CW0%  
Imaginary(S), []

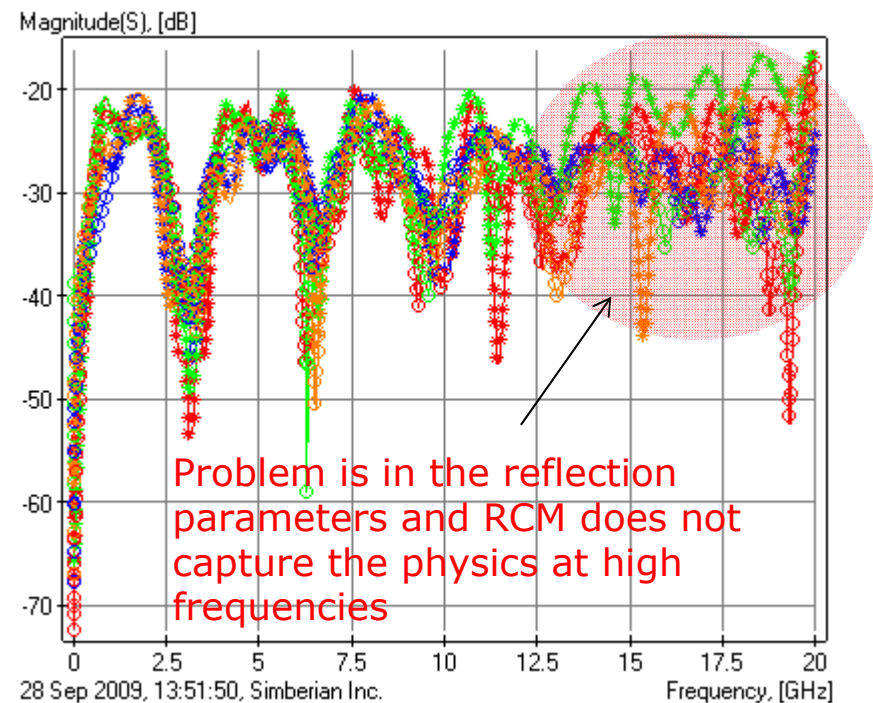
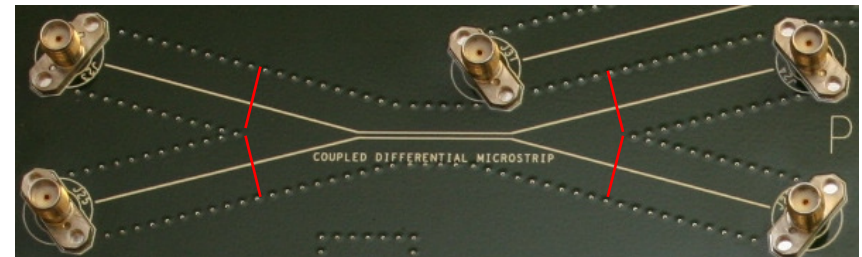
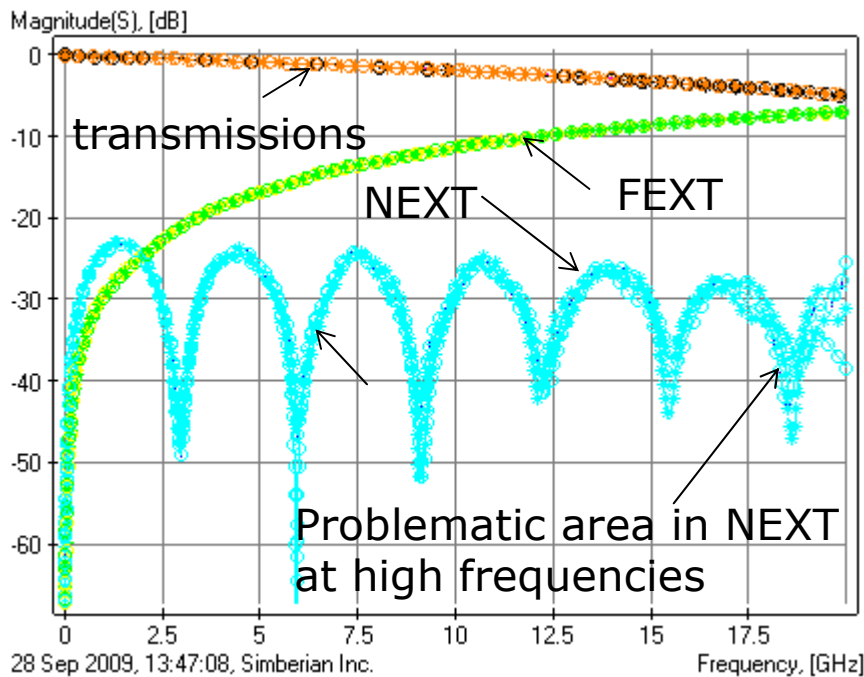


Rotates wrong way!

# Coupled differential micro-strip (TRL): Improving S-parameters with RCM

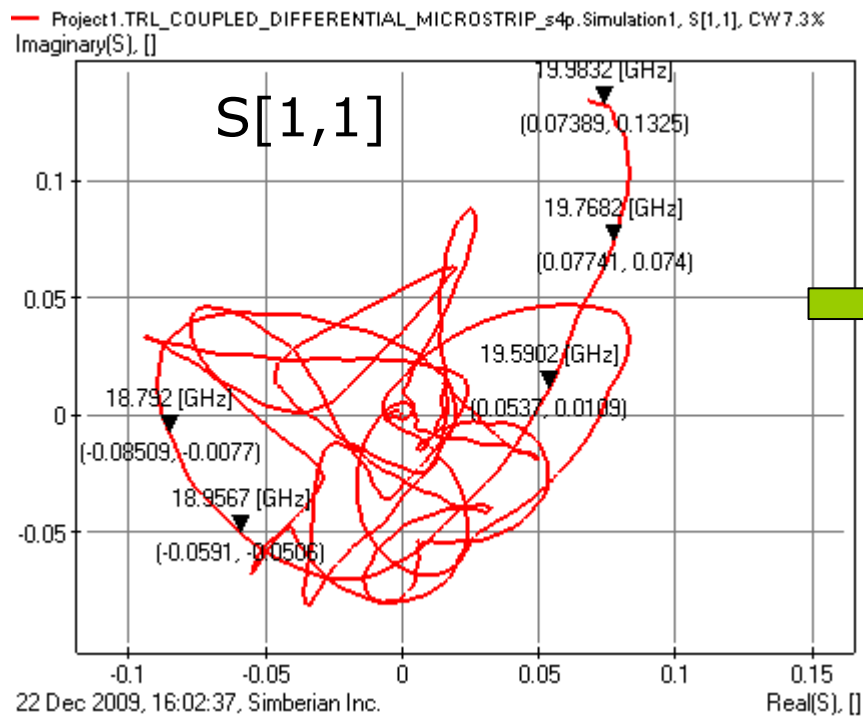
RCM RMS Error is 0.057 (not good)  
Passive from DC to infinity,  
100% causal and reciprocal

VNA - stars RCM - circles



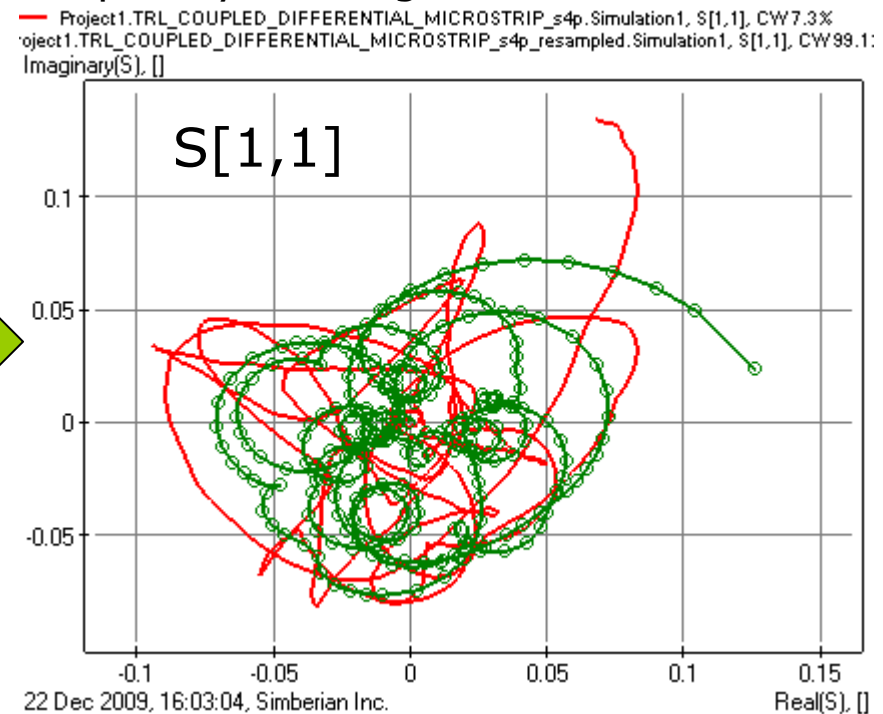
# Coupled differential micro-strip (TRL): Original and improved S[1,1]

VNA Measurement: 3201 points  
starting from 300 KHz



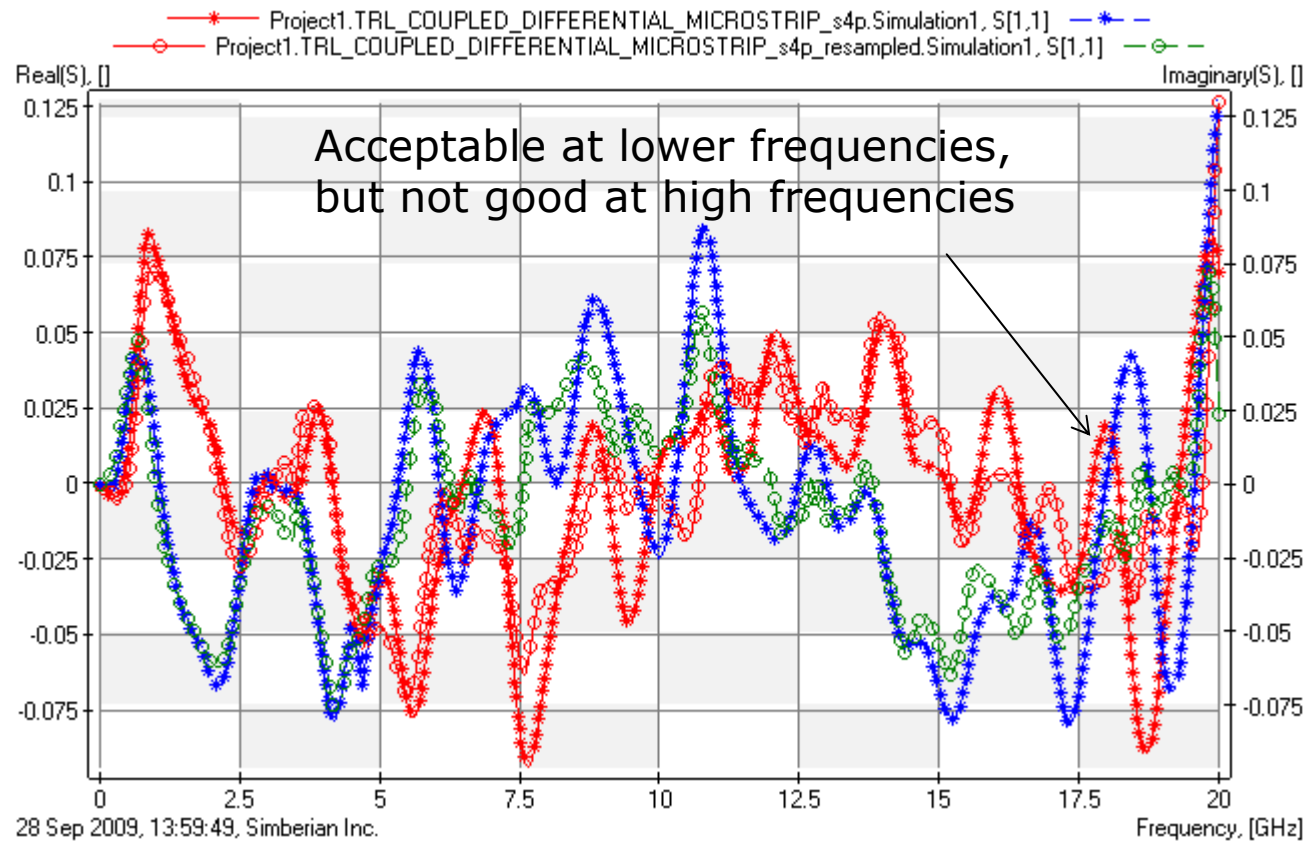
Non-causal data!

Re-sampled RCM: 798 points distributed  
adaptively starting from 0 Hz



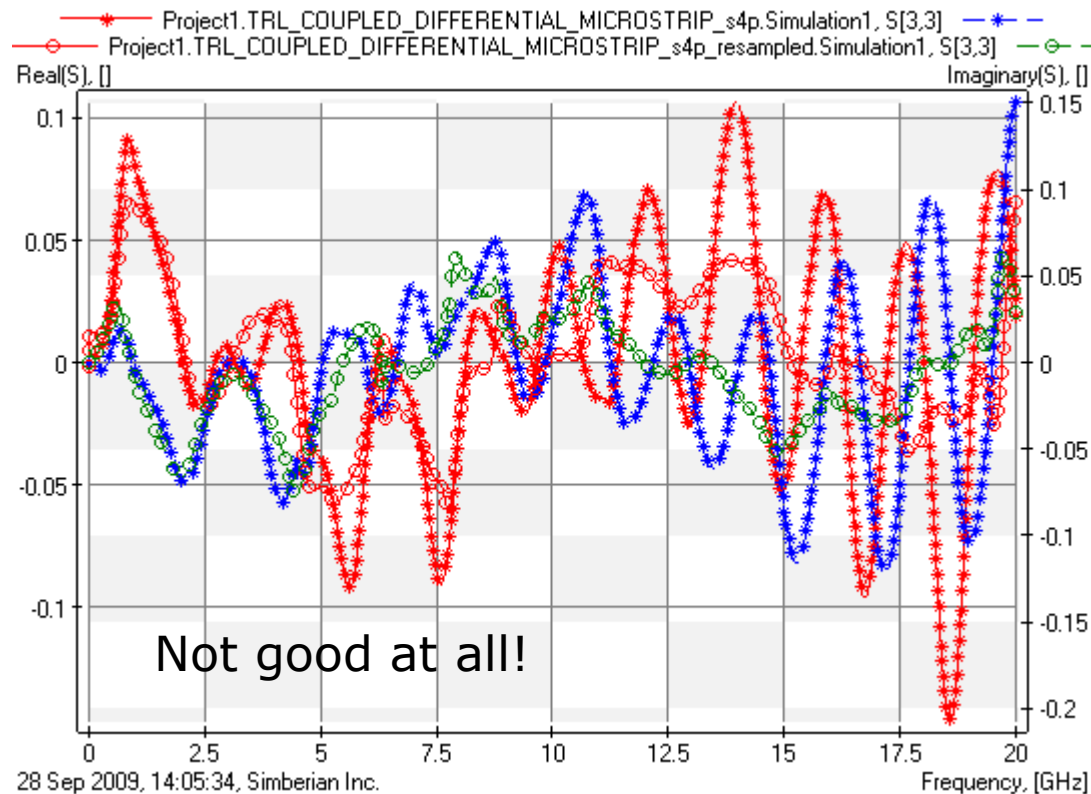
Causal, but may be does  
not capture the physics!

# Coupled differential micro-strip (TRL): Re-sampled RCM vs. original S[1,1]

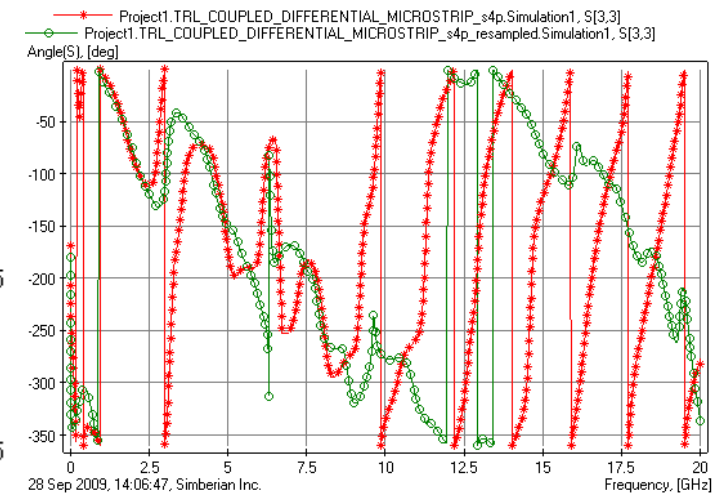


RMS Error 0.031, 40 poles

# Coupled differential micro-strip (TRL): Re-sampled RCM vs. original S[3,3]



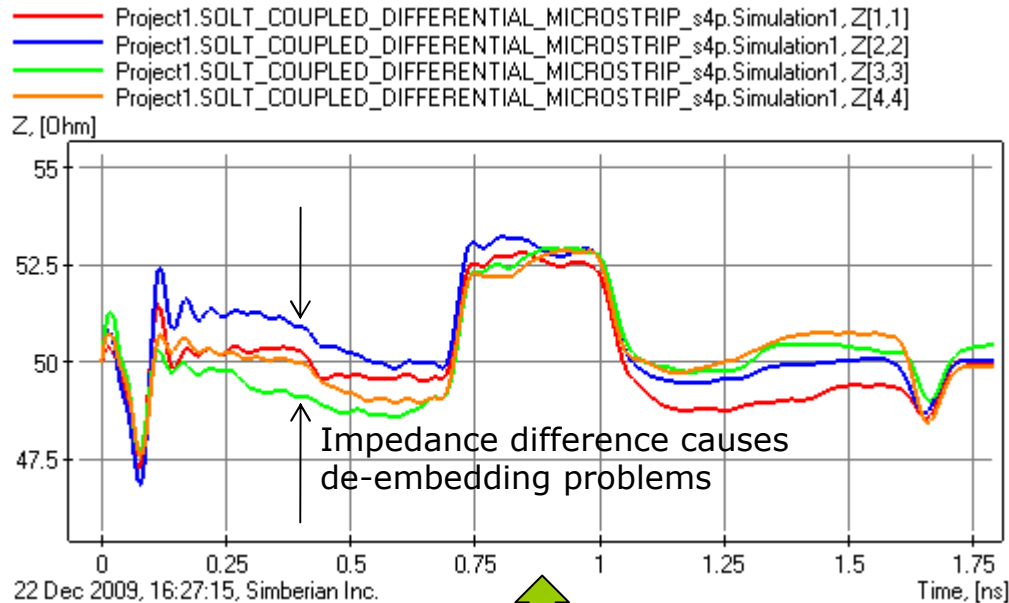
Phase of measured S[3,3]  
goes wrong way starting  
from about 4 GHz



RMS Error 0.057, 29 poles – more poles does not help



# Coupled differential micro-strip (TRL): TDR/TDT from RCM



TDR from SOLT calibrated data (accurate and reliable)

TDR from TRL calibrated data (may be acceptable)

